GRMHD Simulations of Black Hole-Disk Systems

Heavy Element Nucleosynthesis and Implications for r-Process Sites



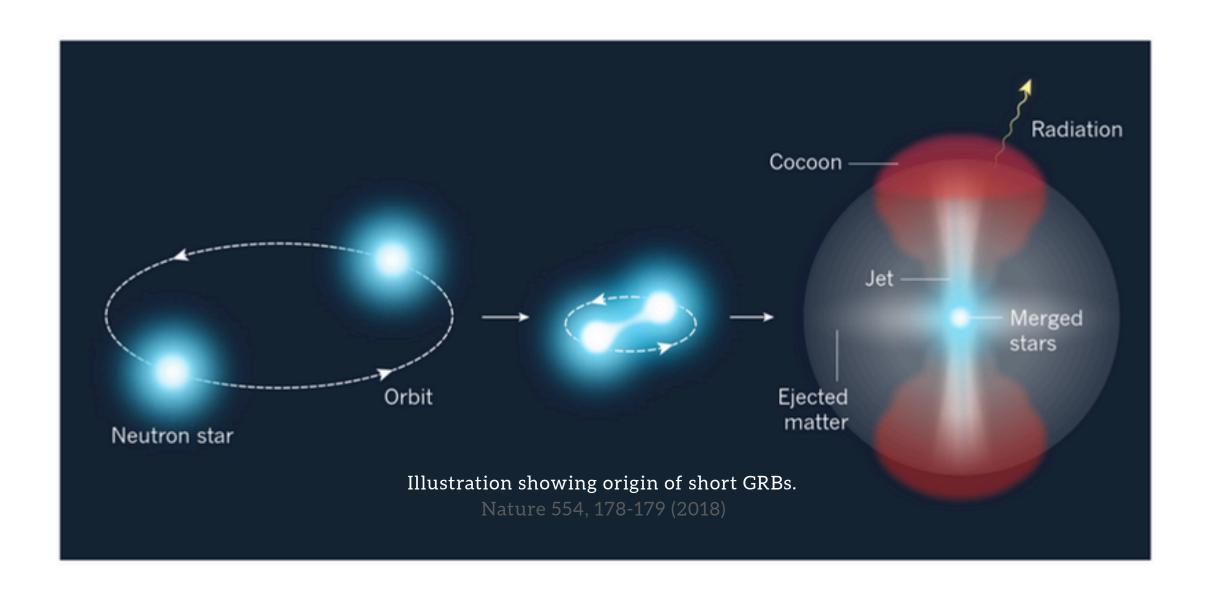
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Short Gamma Ray Bursts (SGRBs)



Transient event that originates from the merger of compact objects; NS-NS; NS-BH (<2s)

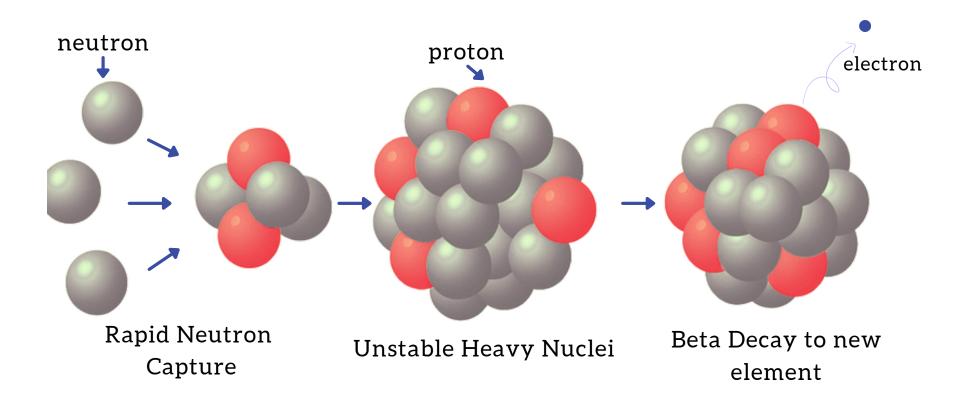
<u>Post-merger environment</u> Black-Hole + Accretion Disk + Disk Wind + Dynamic Ejecta + ultra relativistic jet (GRB)

R-PROCESS NUCLEOSYNTHESIS

Merger Ejecta Dynamic Ejecta + Accretion Disk Winds Highly neutron-rich (Ye ~0.1 - 0.3)

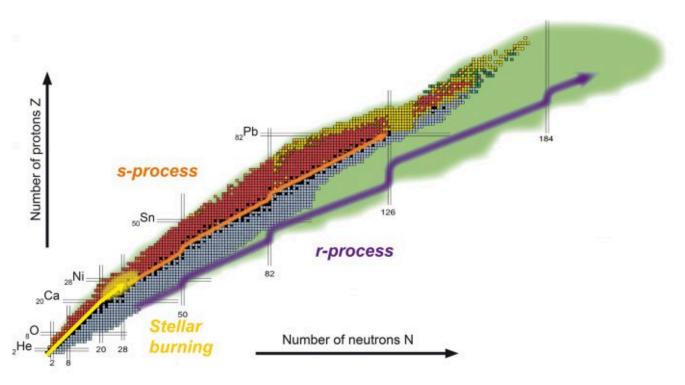
$$Y_{\rm e} = \frac{n_{\rm e}^- - n_{\rm e}^+}{n_{\rm b}}.$$





★ What is R-process

- In neutron-rich ejecta, seed nuclei rapidly capture neutrons, building very heavy, neutron-rich nuclei.
- Followed by β --decay, converting neutrons to protons and stabilizing nuclei into heavy elements.



credit: EMMI, GSI/Different Arts)

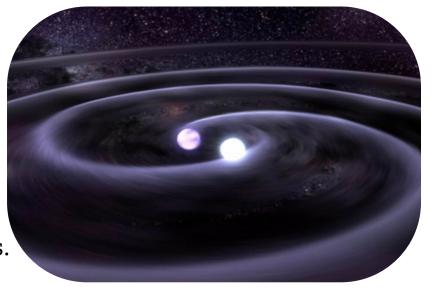
WHY THE R-PROCESS IS IMPORTANT

- Cosmic inventory: \gtrsim 50% of all nuclei heavier than Fe are r-process products; they dominate galactic heavy-element budgets.
- Multi-messenger link: GW events → kilonovae powered by r-process radioactivity; ties gravity, neutrinos, MHD, and nuclear physics.
- Astrophysical Sites of the r-Process
 - **Binary Neutron Star Mergers**: Robust site; confirmed by GW170817 + kilonova (AT2017gfo).
 - NS-WD Mergers proposed sites but possibly low enrichment
 - Core-Collapse Supernovae: Neutrino-driven winds are often too proton-rich; role still debated.
 - *Collapsars & Magnetorotational SNe*: BH + disk systems with strong magnetic fields; potential site for early-universe enrichment.

Conditions for a successful r-process

- Neutron-rich: Ye \leq 0.25 for lanthanides/actinides; higher Ye \rightarrow light-r only (Sr-Ag).
- Fast expansion: ms-s freeze-out (capture decay competes); sets nuclear abundance peak widths/positions.





The Simulation Challenge

A Multi-Stage Approach

Studying nucleosynthesis from mergers is a multi-physics, multi-scale problem (GR, MHD, Neutrino, Nuclear reactions.....)

GRMHD Framework : HARM-EOS

• Solves GRMHD equations in conservative form with finite-volume methods.

Core evolution equations:

• (continuity, energy - momentum conservation, induction equations)

$$\nabla_{\mu}(\rho u^{\mu}) = 0;$$

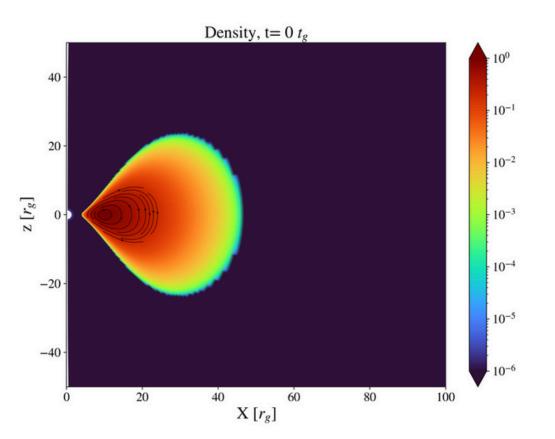
$$\nabla_{\mu}T^{\mu}_{\nu} = Q_{\nu};$$

$$\nabla_{\mu}F^{\mu\nu} = 0;$$

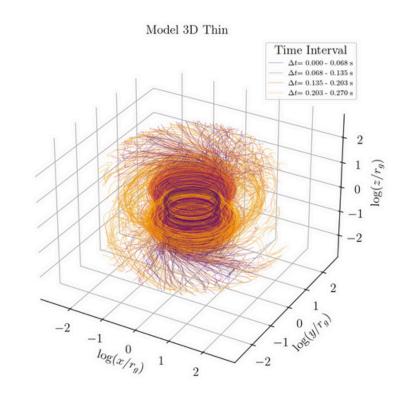
$$\partial_{t}\mathbf{U}(\mathbf{P}) = -\partial_{i}\mathbf{F}^{i}(\mathbf{P}) + \mathbf{S}(\mathbf{P})$$

- Neutrino Cooling:
- Leakage scheme computes a gray optical depths for neutrinos (v_e, \bar{v}_e, v_x)
- Q_{ν} energy change due to neutrino cooling (in conservation equations)
- Equation of State (EOS)
- Tabulated 3-parameter EOS: ε(ρ,T,Ye) P(ρ,T,Ye)
- Additional modules are available with self-gravity implementations

Initial Setup - Rotating kerr BH + Accretion Disk (Poloidal B)



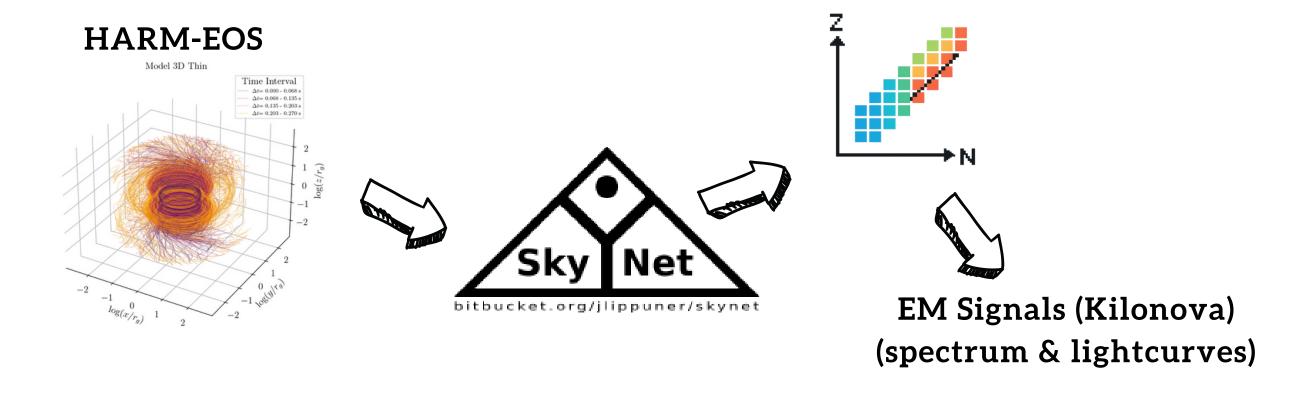
Accretion disk density profile with Magnetic field streamlines at time=0; (Model 3D-Kn)



Tracer particle - records properties like density, temperature, electron fraction, coordinates & time to track the disk winds and used in Skynet to calculate nuclear abundance

Nuclear Reaction Network Code: SKYNET

(Post processing of GRMHD results to calculate abundance profiles)



- General-purpose nuclear reaction network
- ◆ Tracks >7 000 nuclides, ~140 000 reactions
- Accepts tracer histories ρ(t), T(t),
 Ye(t) from HARM-EOS
- Returns time-resolved abundances, heating rates
- ◆ Supports coulomb screening, self-heating & v-driven Ye evolution

SkyNet - compute the nucleosynthesis evolution in all astrophysical scenarios where nucleosynthesis occurs.

Proper elemental abundance combined with nuclear opacities is crucial for detailed studies of EM signals following this event.

Further radiation transport helps us study the EM emission following these events.

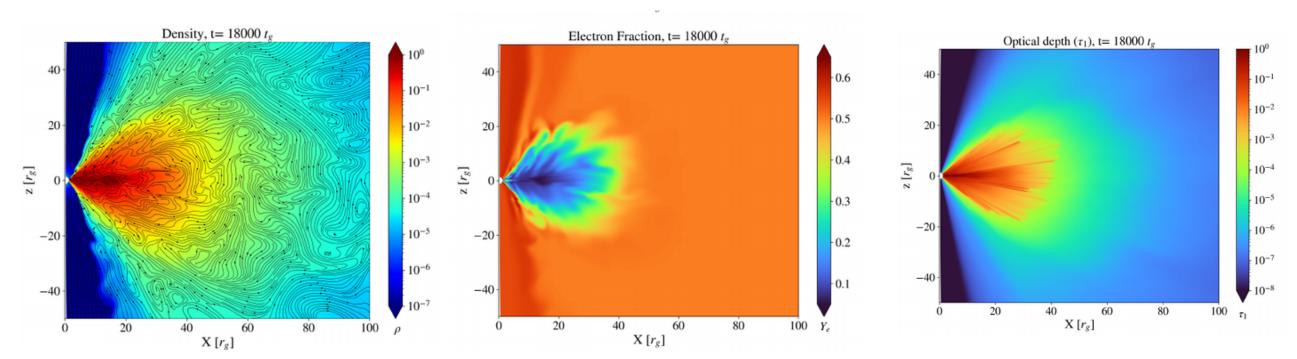
Post-Merger Simulations - Results

- AIM Study how the Post-merger Accretion disk properties evolve & affect heavy element formation & Resulting EM Transient
- 3-D & 2D v-GRMHD with HARM-EOS composition-dependent, 3-parameter EOS + neutrino-leakage; Magnetised jet production, and self-consistent Ye evolution.
- The current simulation properties focus on the BNS and NS-BH merger scenario & some models are fine-tuned to reproduce kilonova emission followed by GRB 211211A.
- ~10⁵ tracers are initialised to follow unbound winds; record (ρ, T, Ye); trajectories post-processed with SkyNet.

Simulation Parameters -

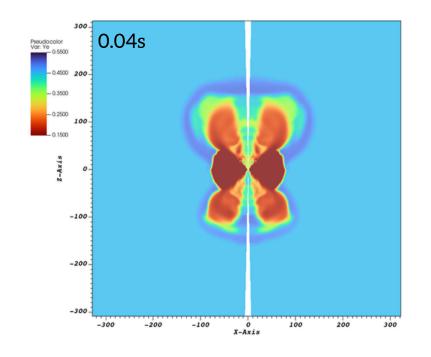
9 Models - 2D & 3D simulations

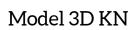
- BH spin, a = 0.6 0.9,
- BH mass, 3 8 M☉,
- Accretion disk mass ~0.001 ~0.1 M☉,
- plasma $\beta \sim 50 100$
- disk entropy 7-10 kB per baryon;



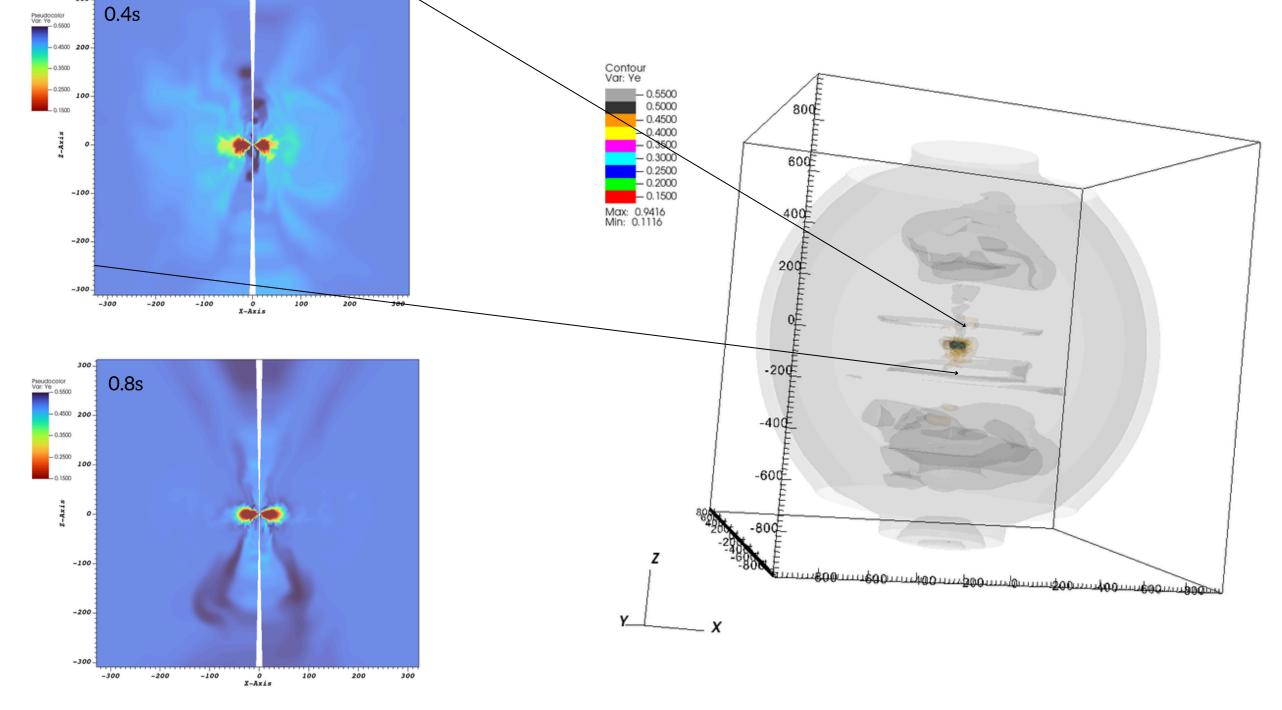
Accretion Disk snapshots at a later time of evolution (Model 2D-Thin) (~0.3s in real time)
Left Panel: Density + Magnetic field lines, Mid Panel- Ye; Right Panel - Neutrino optical depth

Ye Evolution - Model 3D-Kn

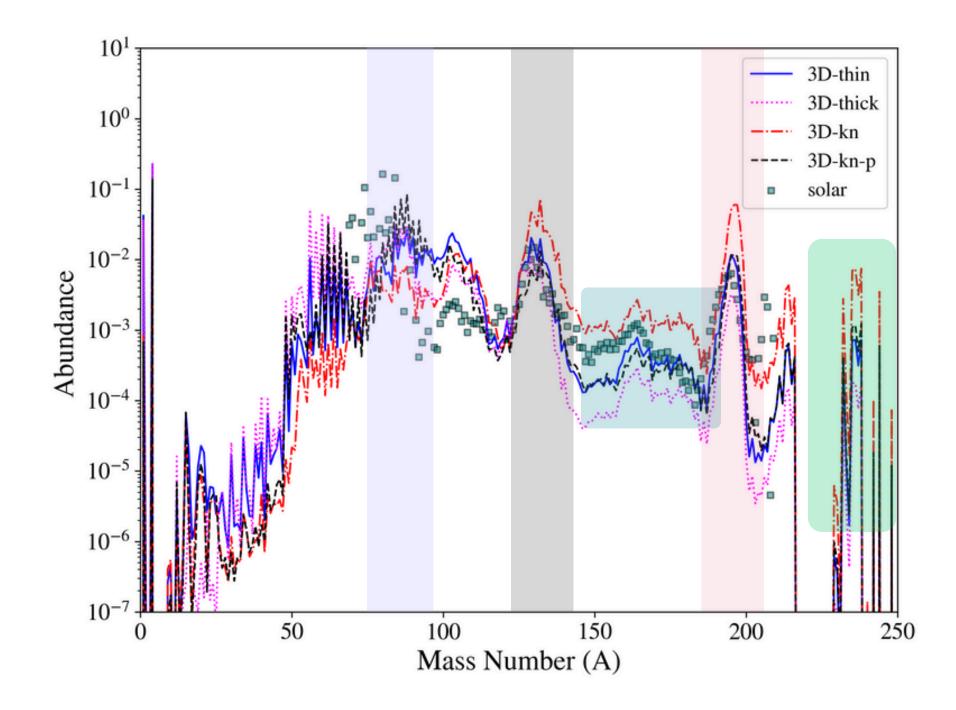




- BH spin, a = 0.6
- BH mass, 8 M☉,
- disk mass ~0.781M ⊙,
- plasma β ~ 50



Nuclear Abundance Profiles



Nuclear Abundance profiles of four 3D models in this work. Models succeed in reproducing solar r-process peaks.

Models reproduce prominent r-process peaks 1st A~95 (Sr,Zr..), 2nd A~130 (Xe,Sn..), 3rd A~195 (Pt, Au..) lanthanides (Nd, Eu..) & Actinides (Th, U..)

Model	Mass Ejecta (M☉)	<ye> (10 GK)</ye>	Velocity (1/c) (500 rg)
3D-Thick	2 x 10 ⁻²	0.42	0.13
3D-Thin	2 x 10 ⁻³	0.37	0.10
3D-kn	1 x 10 ⁻¹	0.20	0.07
3D-kn-p	2 x 10 ⁻³	0.37	0.19

NS Merger R-Process → Responsible for formation more than 50% of Universes heaviest Elements

R-process & Kilonovae

Merger Scenario - Heavy Element production

- Disk Winds (post merger) + Dynamic Ejecta (pre Merger)
 - Radioactive decay of heavy elements Power Transient
 - electromagnetic transient from r-process → (Li & Paczy'nsky 1998)
 - GW170817 Discovery of kilonovae (Overlapping GRB afterglow; Optical IR; timescale ~days)
 - Modeling Kilonova Emission required a detailed understanding of ejecta properties + Radiation Transport

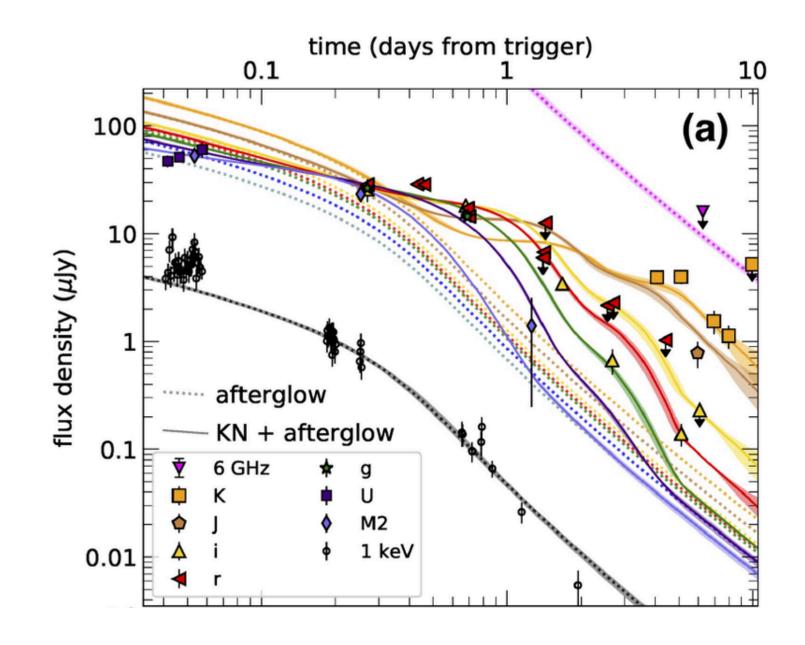
Two & Three Component Analytical KNe Modelling

✓ Dynamical ejecta → Neutron-rich, heavy r-process elements (lanthanides, actinides, high opacity) Red Kilonova

✓ Disk wind ejecta→ Moderately neutron-rich, light/heavy r-process elements Blue Kilonova

GW170817 / AT2017gf Blue - Mej = 0.02, v= 0.25c Red - Mej = 0.05, v= 0.15c

Our simulation Models produce ---Total disk M_ejecta ranging 10⁻³ - 10⁻¹ ⊙
Velocities: 0.05 - 0.20 c



Kilonova observation: GRB 211211A Source: Rastinejad, J.C., et al .(2022).

Ejecta produced have properties in the range sufficient to produce observed kilonovae properties; Detailed Radiation Transport - Planned/ongoing

Summary

- 3D simulations of post-merger accretion disks with multiple initial configurations were carried out using the new HARM-EOS 3D v-GRMHD code, developed at CTP PAS.
- Post-processing using Skynet nuclear reaction network shows that accretion disk winds robustly produce heavy r-process (A \gtrsim 100); yields (10⁻³–10⁻¹ M \odot) of ejecta with velocities (0.1 0.2c).
- Post-merger disk properties significantly impact the microphysics of ejecta and, consequently, the production of heavy elements (We found 1-3 orders of difference in heavy element ratios between different models).
- Abundance profiles from simulations match solar abundance, and the velocity/ejecta properties are consistent with powering a GW170817-like kilonova.

Thank You

Ye: 3Dkn

