

# Gravitational wave signals from Long Gamma Ray Bursts jets

**Gerardo Urrutia**

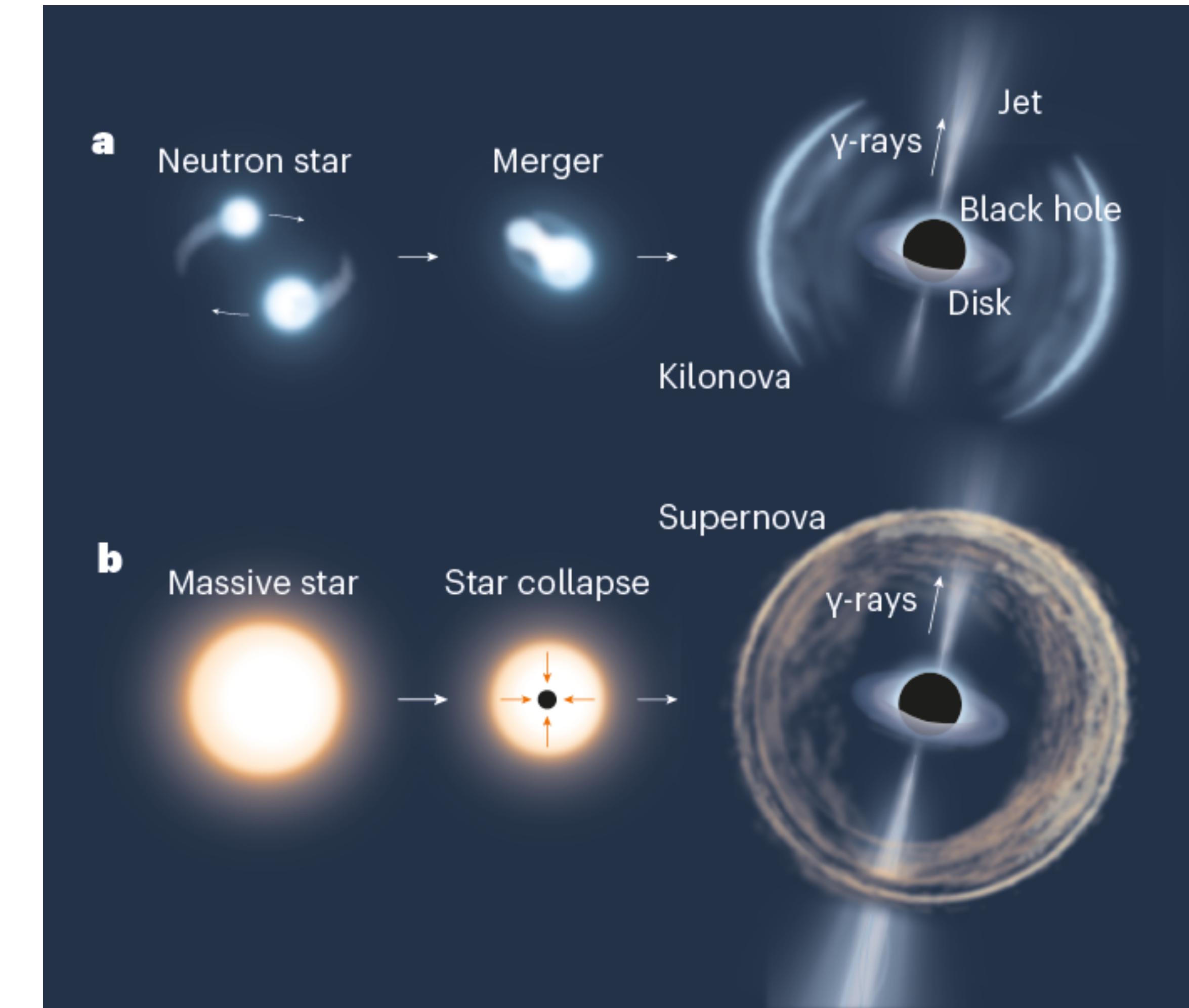
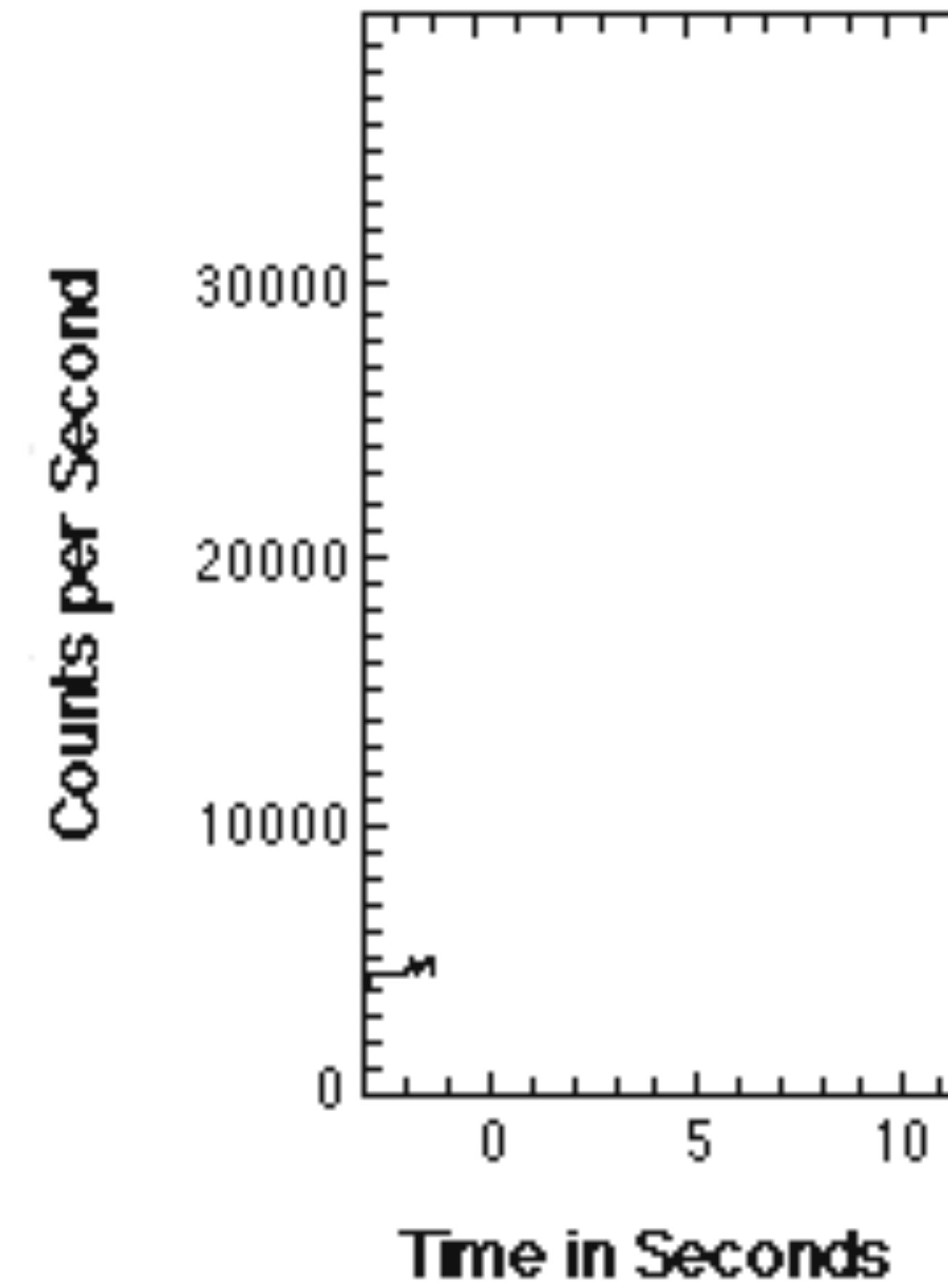
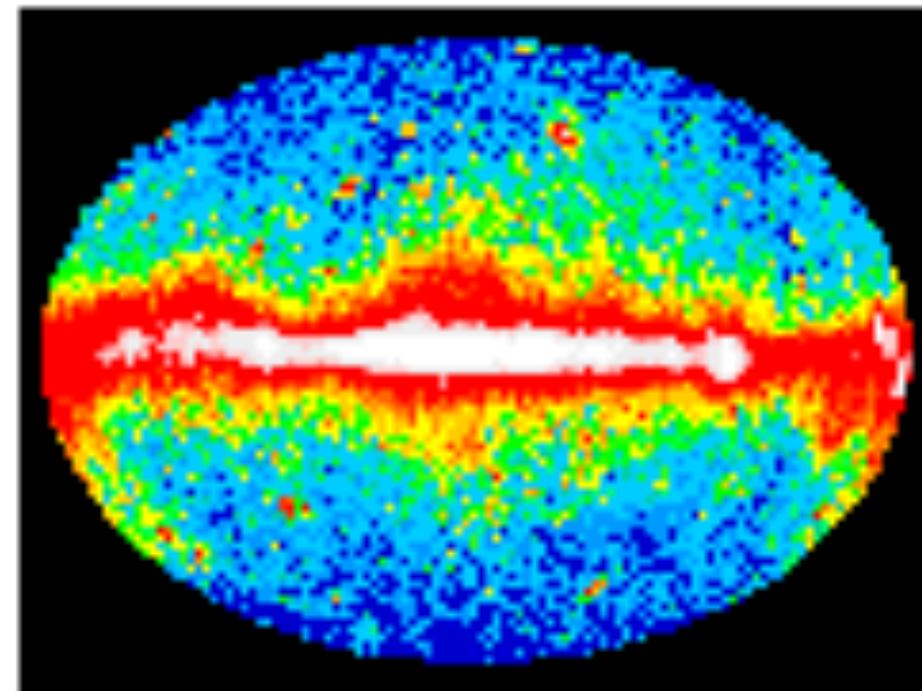
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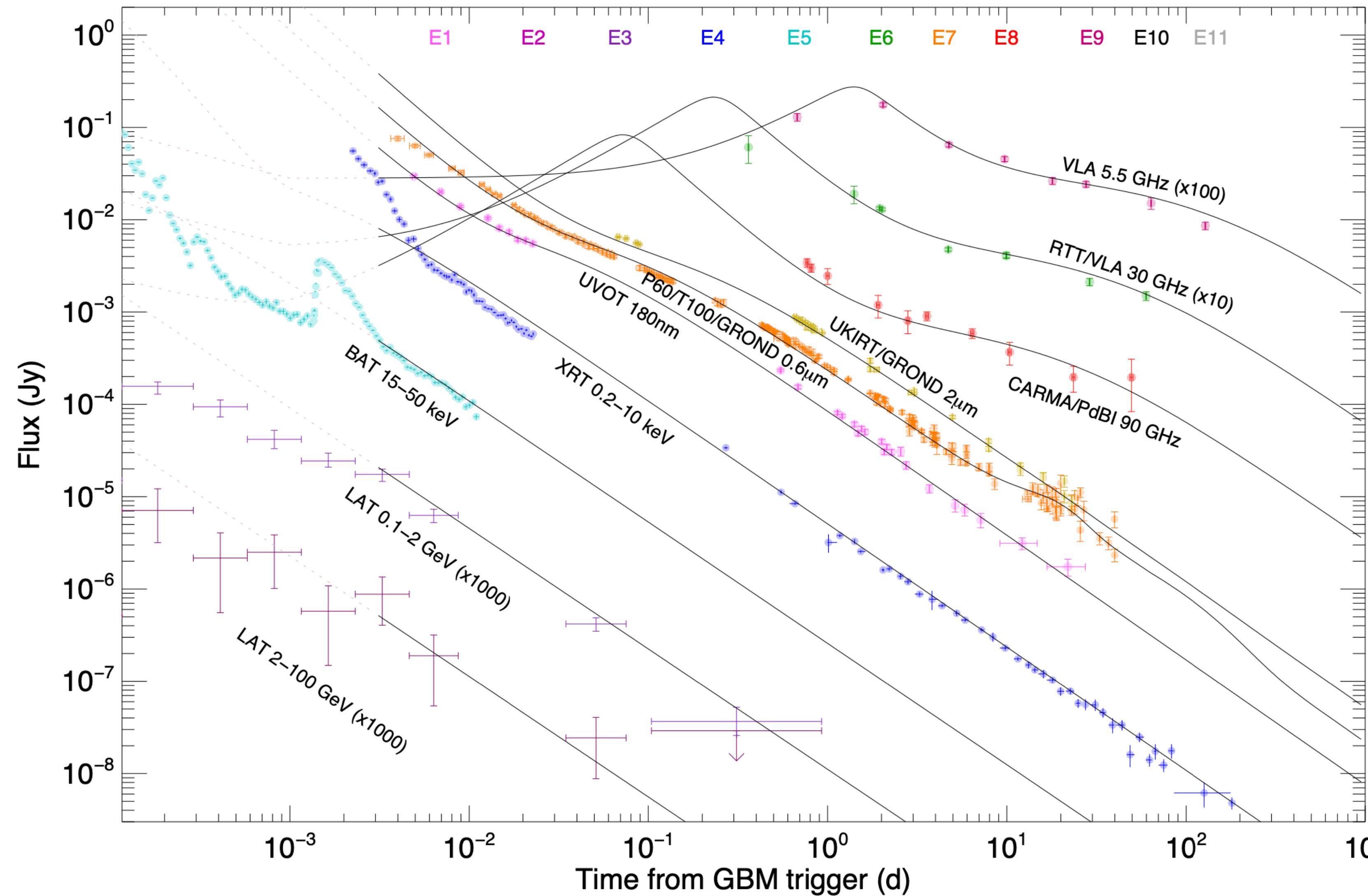
**Agnieszka Janiuk (CFT, Poland), Fabio De Colle (UNAM, Mexico),  
Claudia Moreno (UdG, Mexico), Michele Zanolin (ERU, USA)**

Seminario Instituto de Astronomía, Universitat de València, June 17th 2024

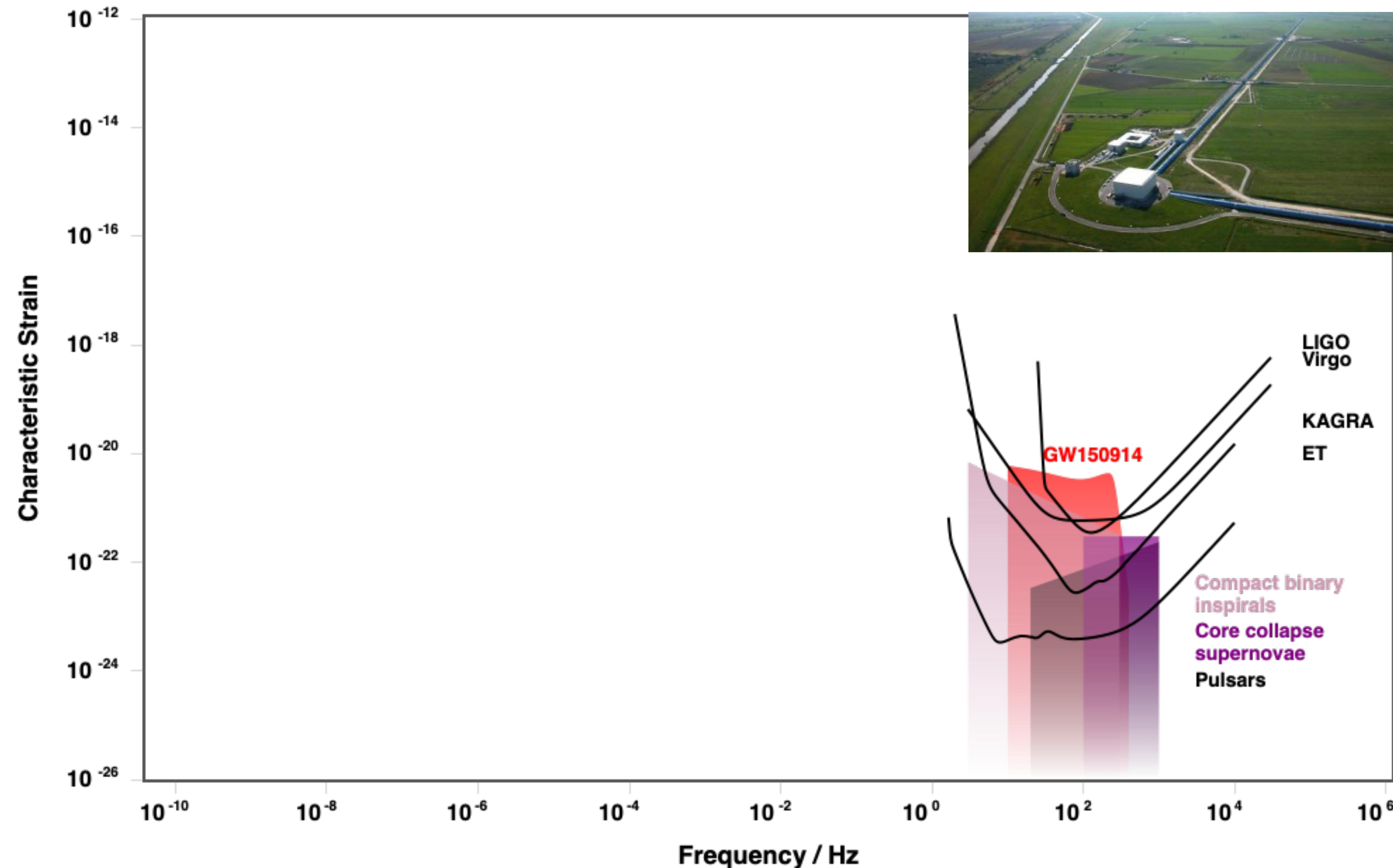
# Prompt emission and Progenitors

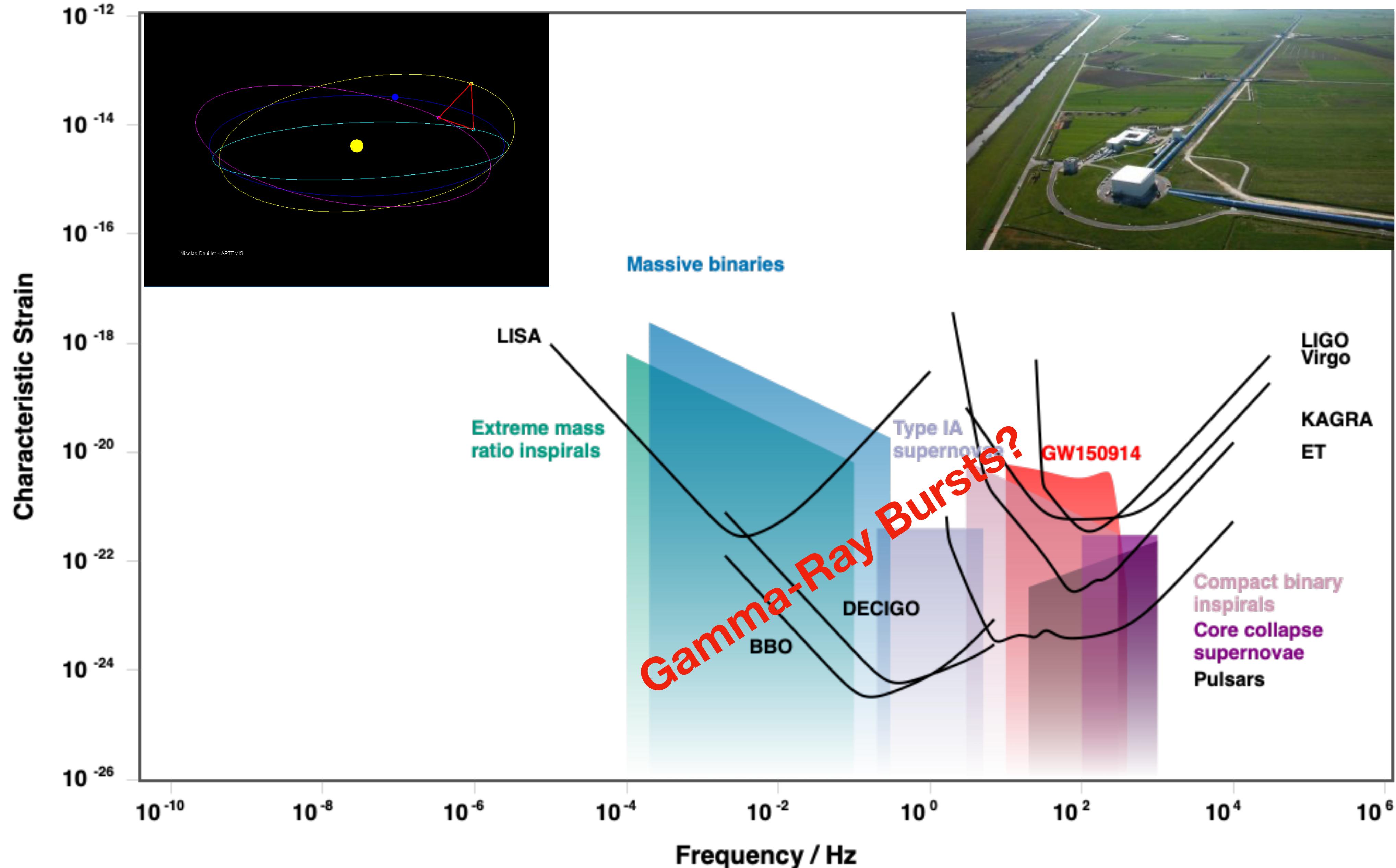


# Gamma-Ray Bursts (afterglow emission)



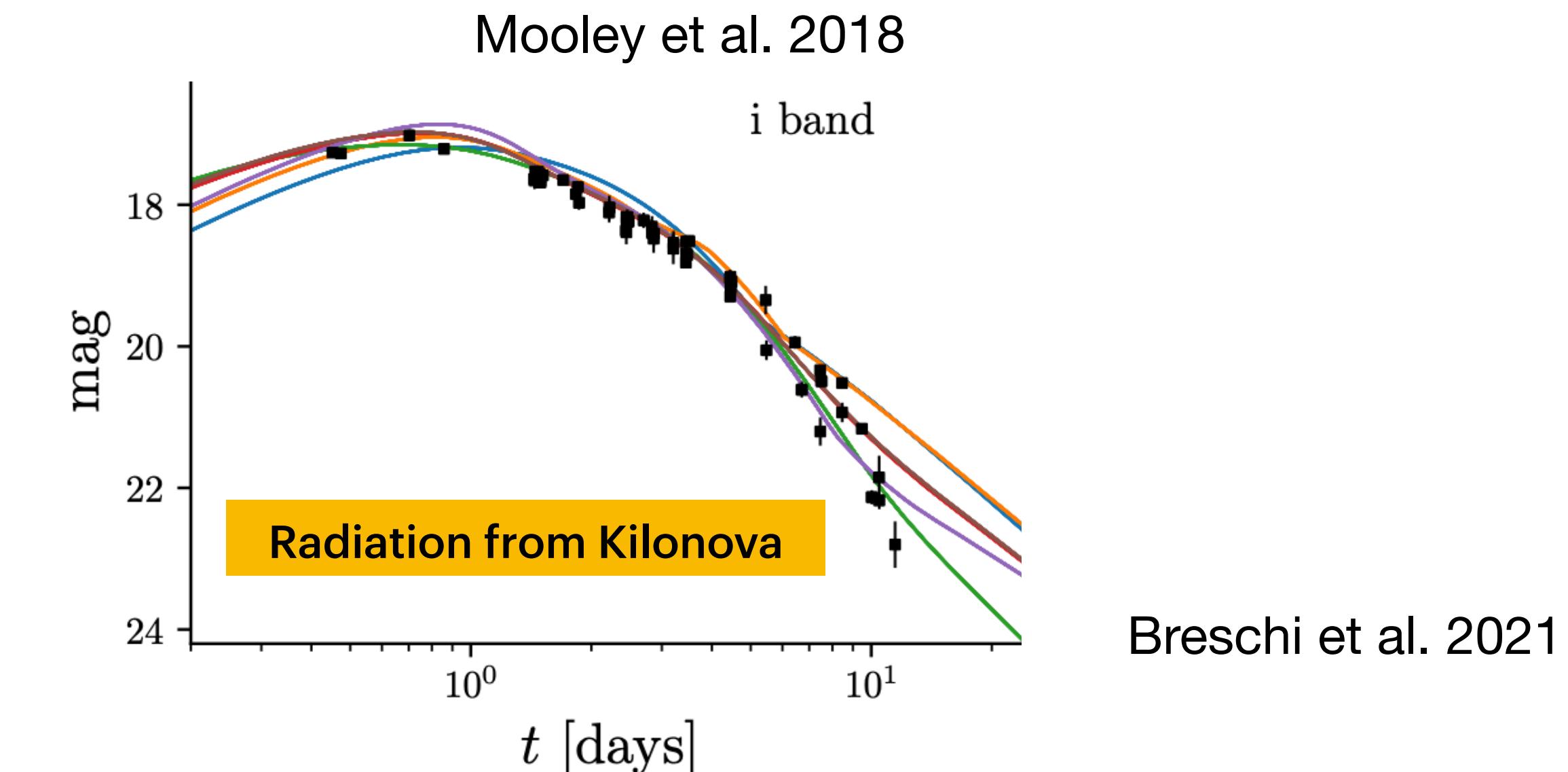
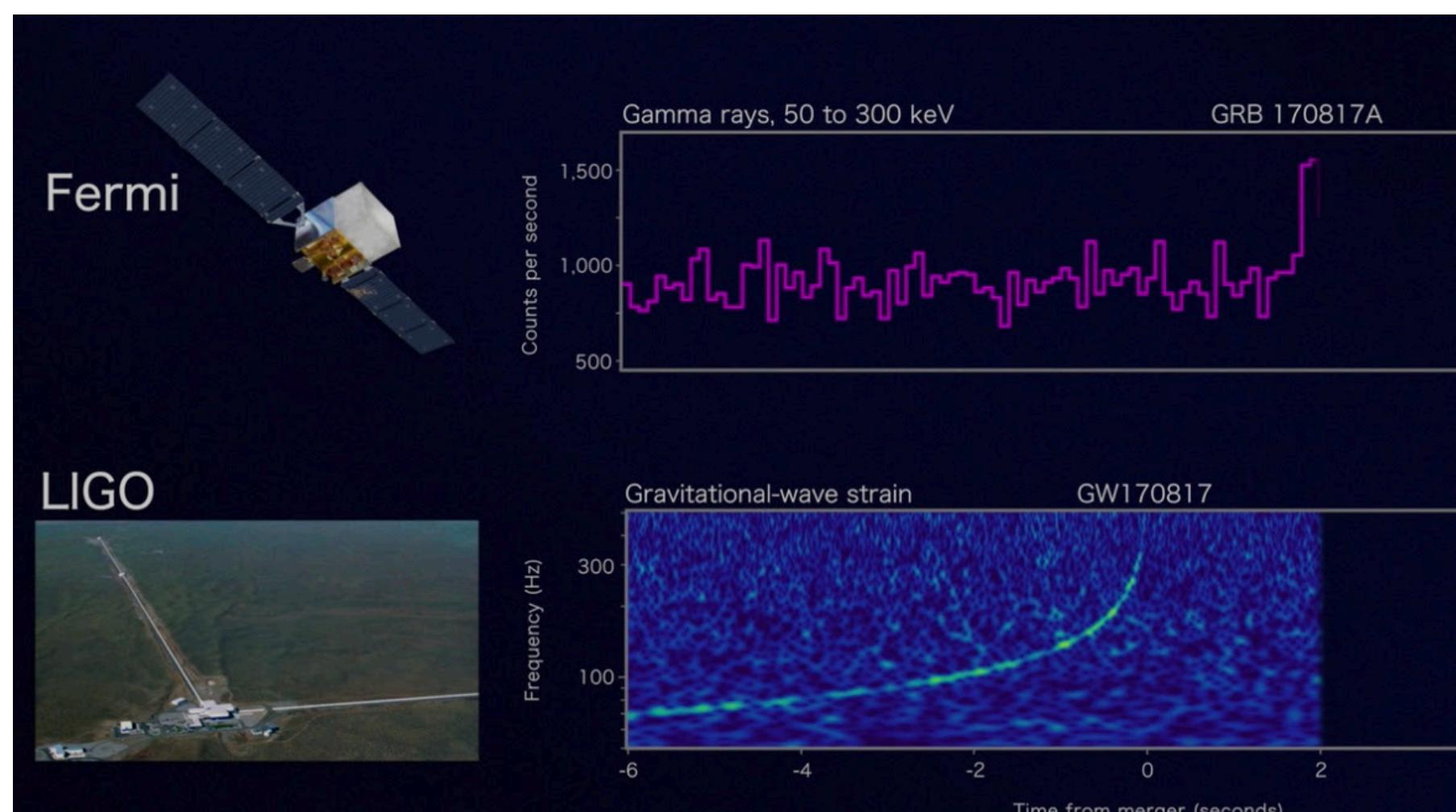
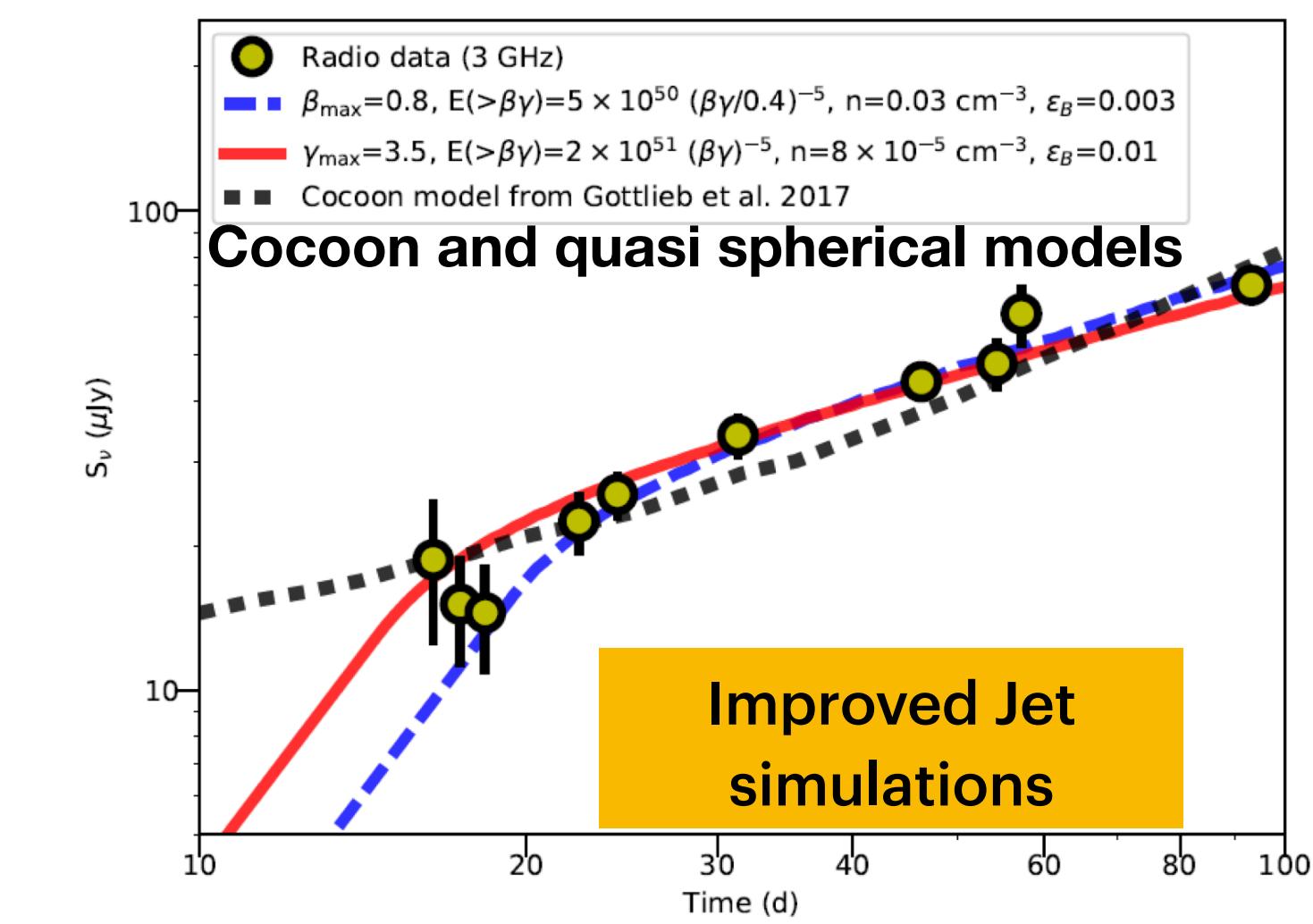
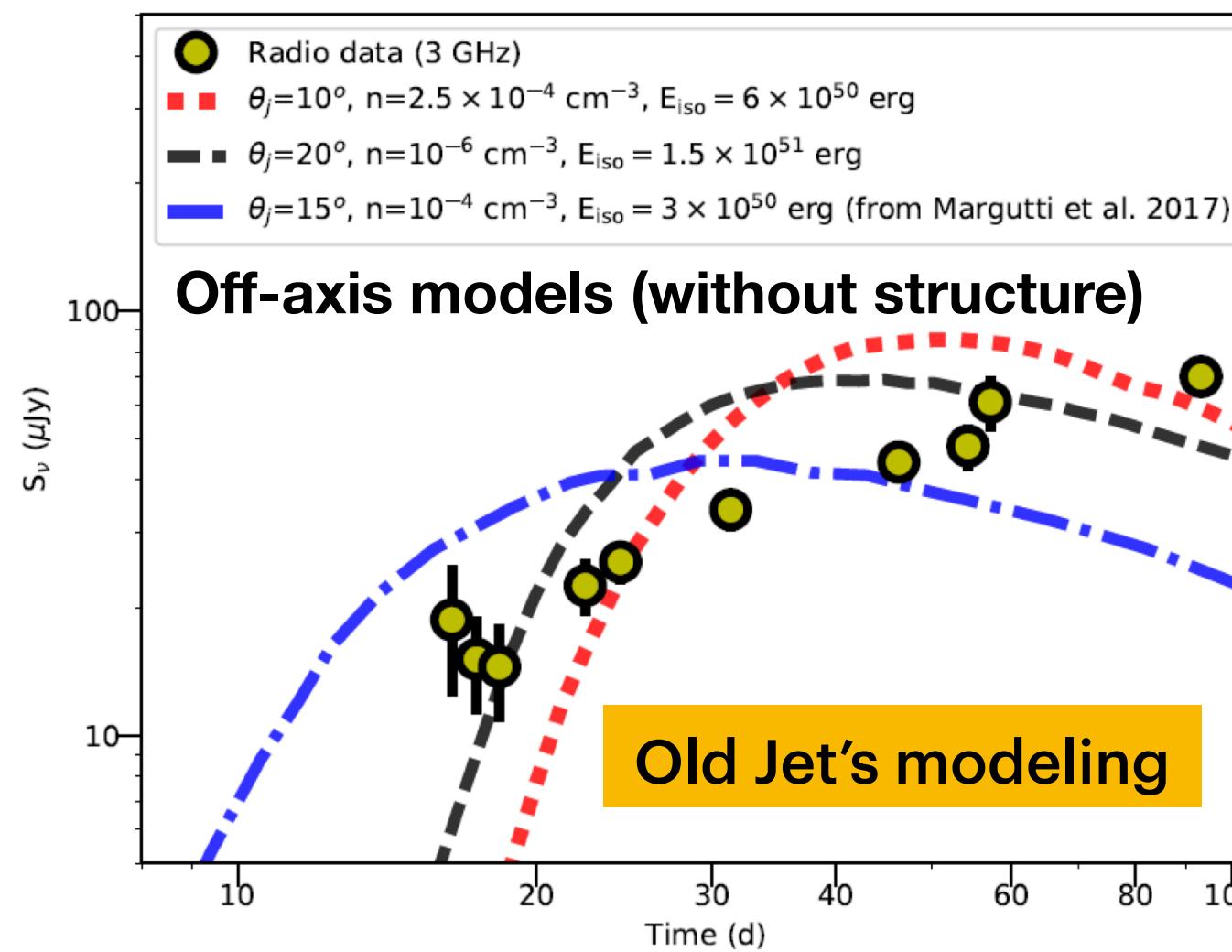
GRB 130427, Perley et al. 2013

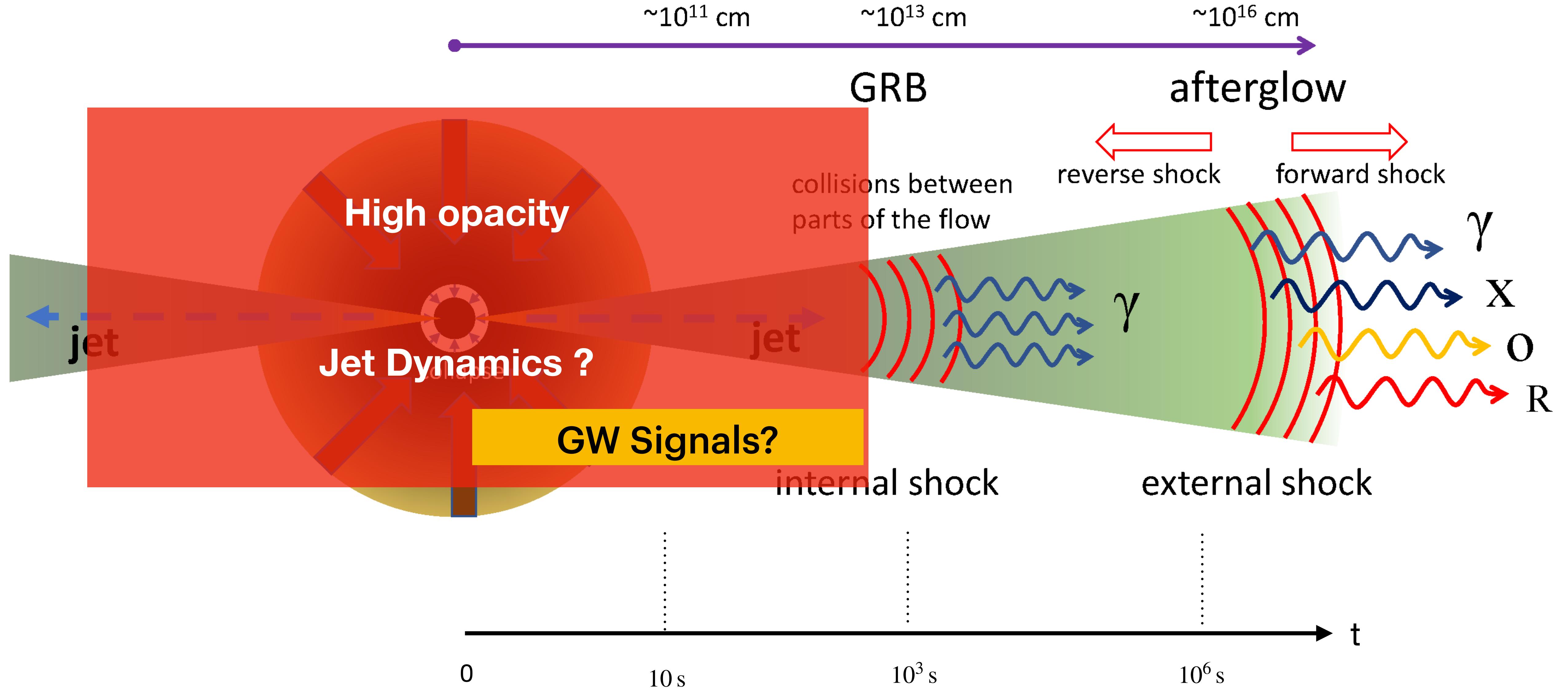




# Multi-messenger Astrophysics

## Non-photonic signals + Electromagnetic counterparts

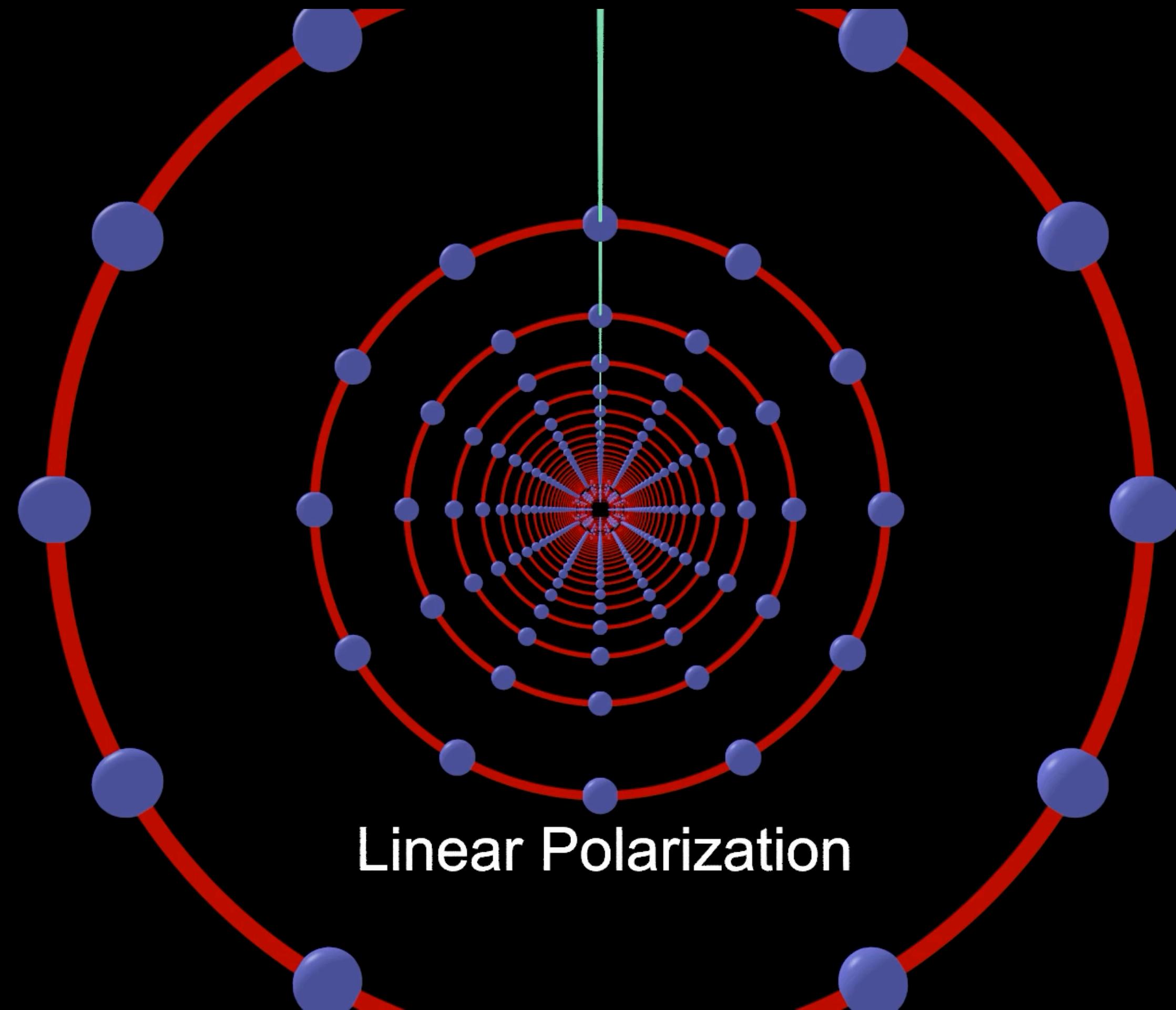




# Gravitational waves

$h_+$  → linear

$h_x$  → circular



$$h \sim \frac{G}{c^4} \frac{E_{\text{GW}}}{d} \sim 10^{-21}$$

# GW signal from a radiating point mass

$$h_+ \equiv h_{xx}^{TT} = -h_{yy}^{TT} = \frac{2G}{c^4} \frac{E}{D} \frac{\beta^2 \sin^2 \theta_\nu}{1 - \beta^2 \cos \theta_\nu} \cos 2\Phi$$

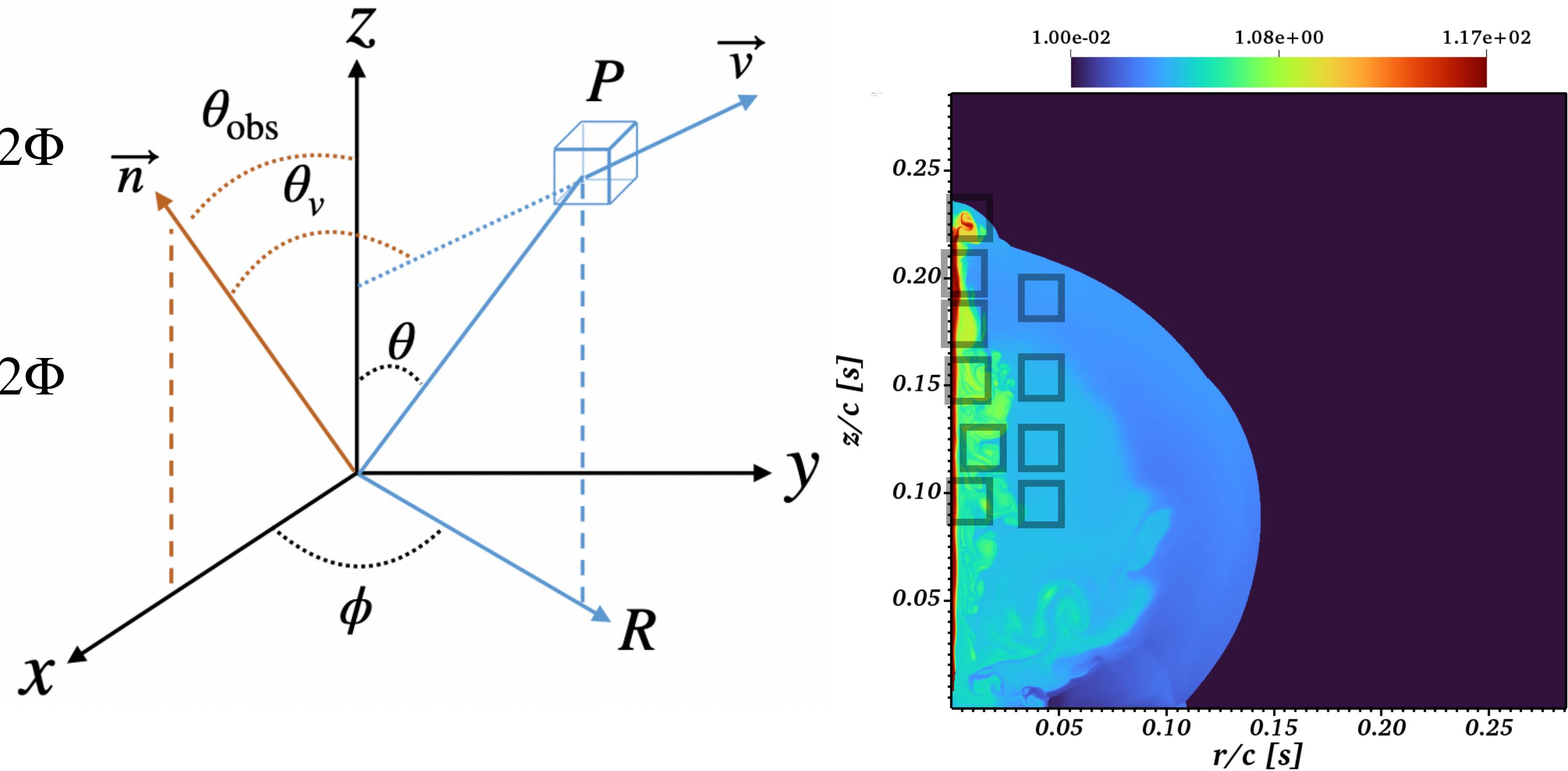
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Braginskii & Thorne 1987,

Segalis & Ori 2001,

Birnholtz & Piran (2018),

Leiderschneider & Piran 2021

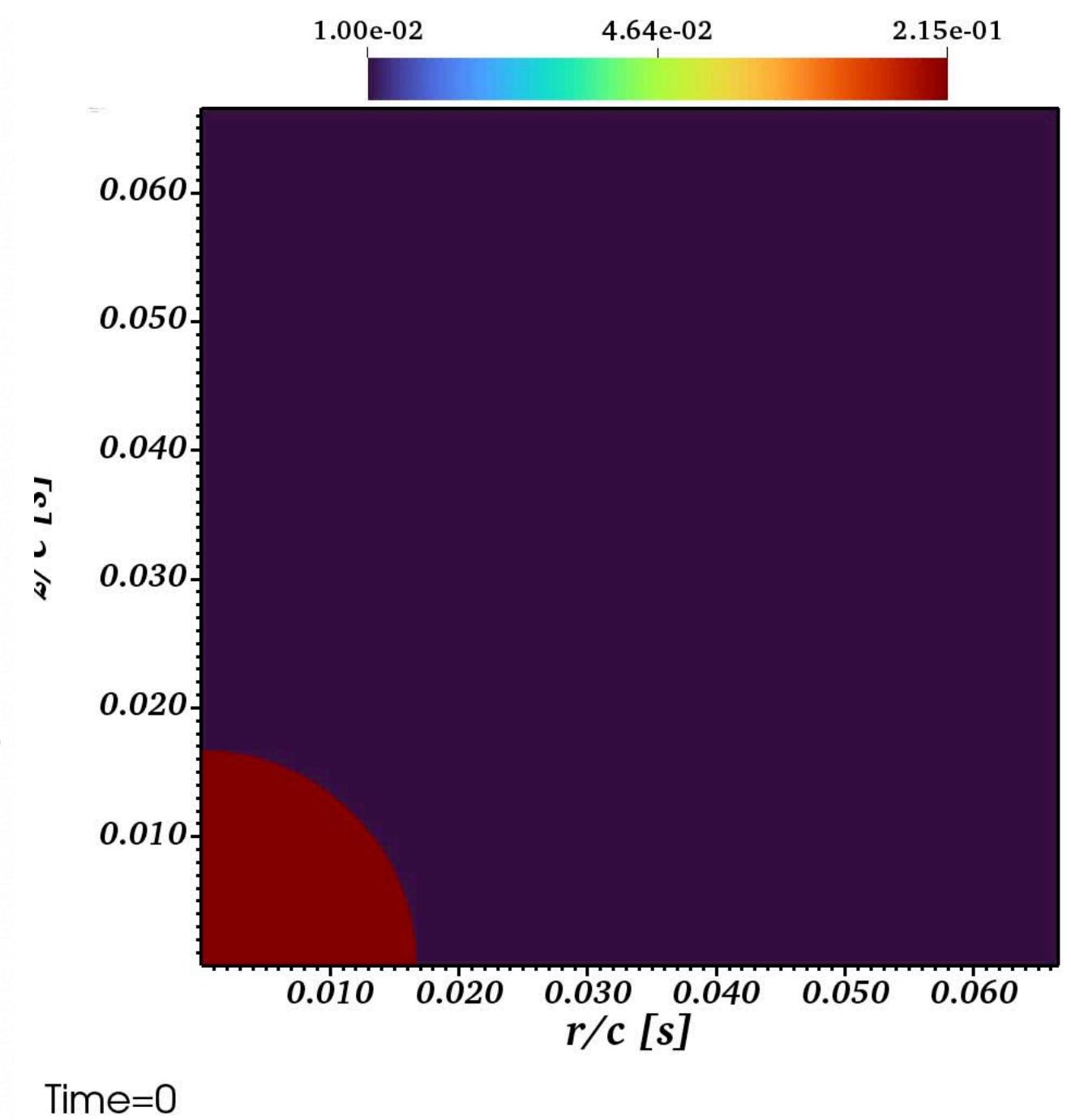
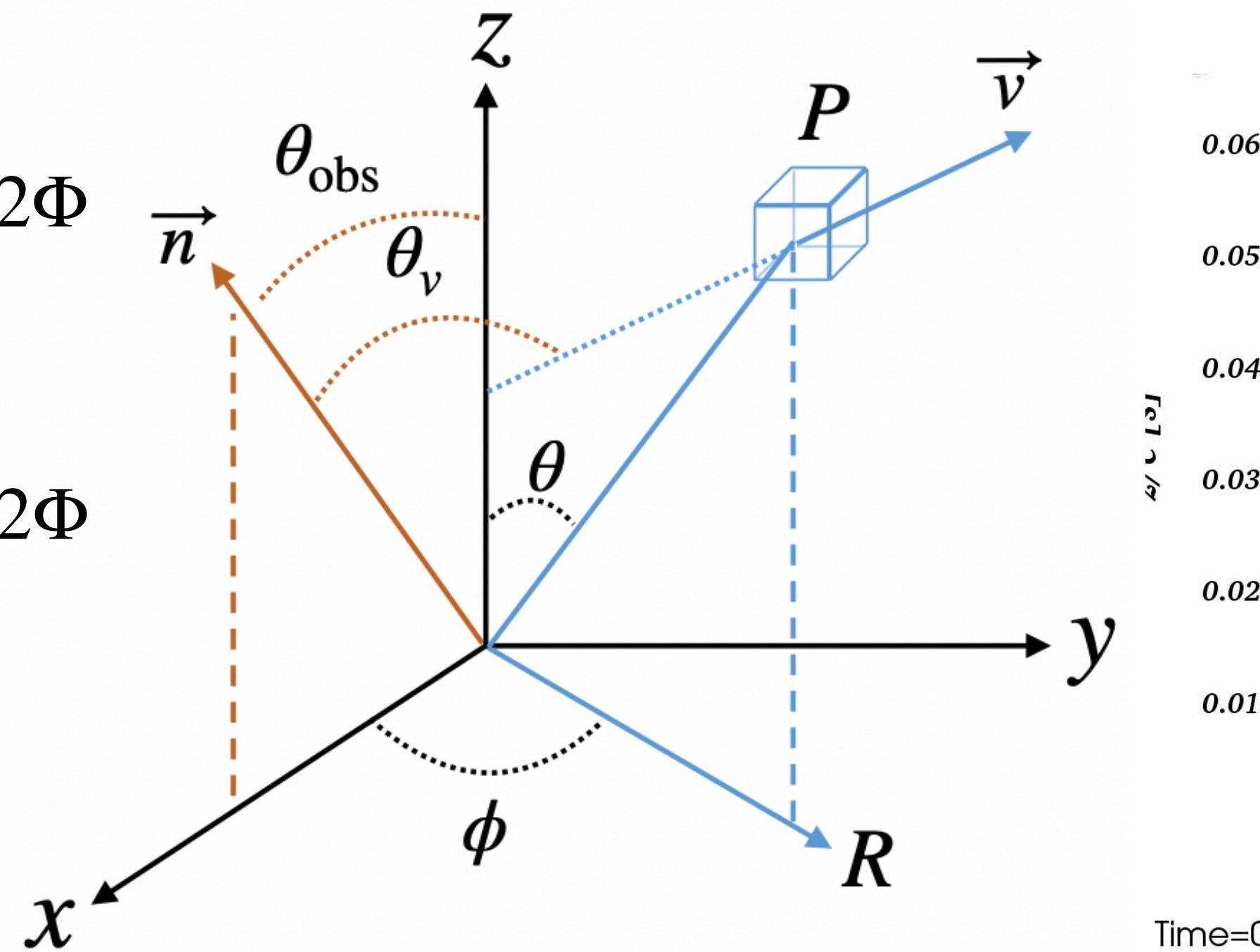


$$\cos \theta_\nu = \hat{n} \cdot \hat{\beta} = (\beta_R \sin \theta_{\text{obs}} \cos \phi + \beta_z \cos \theta_{\text{obs}}) / \beta$$

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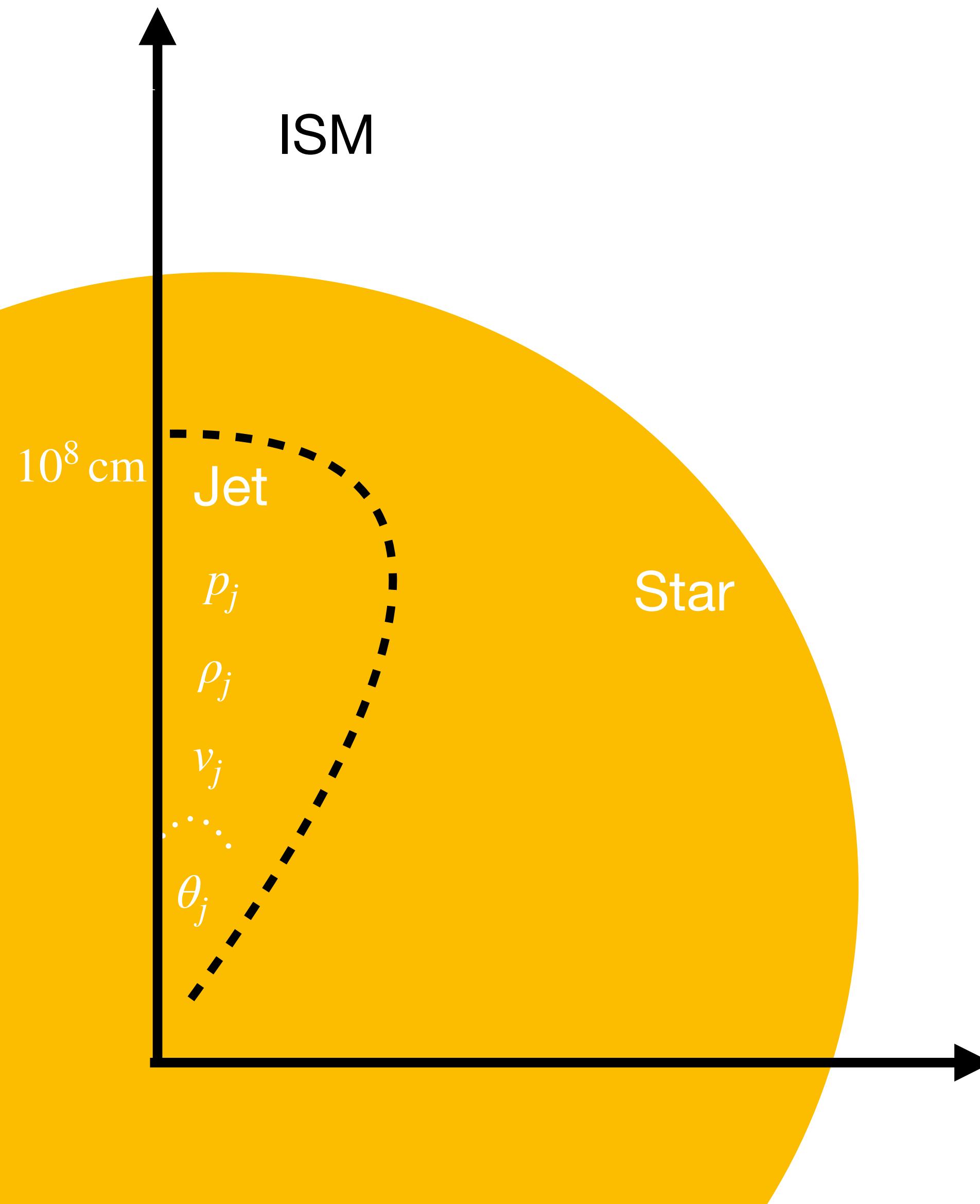
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$$\cos \theta_\nu = \hat{n} \cdot \hat{\beta} = (\beta_R \sin \theta_{\text{obs}} \cos \phi + \beta_z \cos \theta_{\text{obs}}) / \beta$$

# Initial conditions

(Mezcal Code: De Colle et al. 2012)



$$\frac{\partial \mathbf{U}}{\partial t} + \frac{\partial \mathbf{F}^i}{\partial x^i} = 0$$

$$\mathbf{U} = (D, m_j, \tau)$$

$$\mathbf{F}^i = (Dv^i, m_j v^i + p \delta_j^i, \tau v^i + p v^i)$$

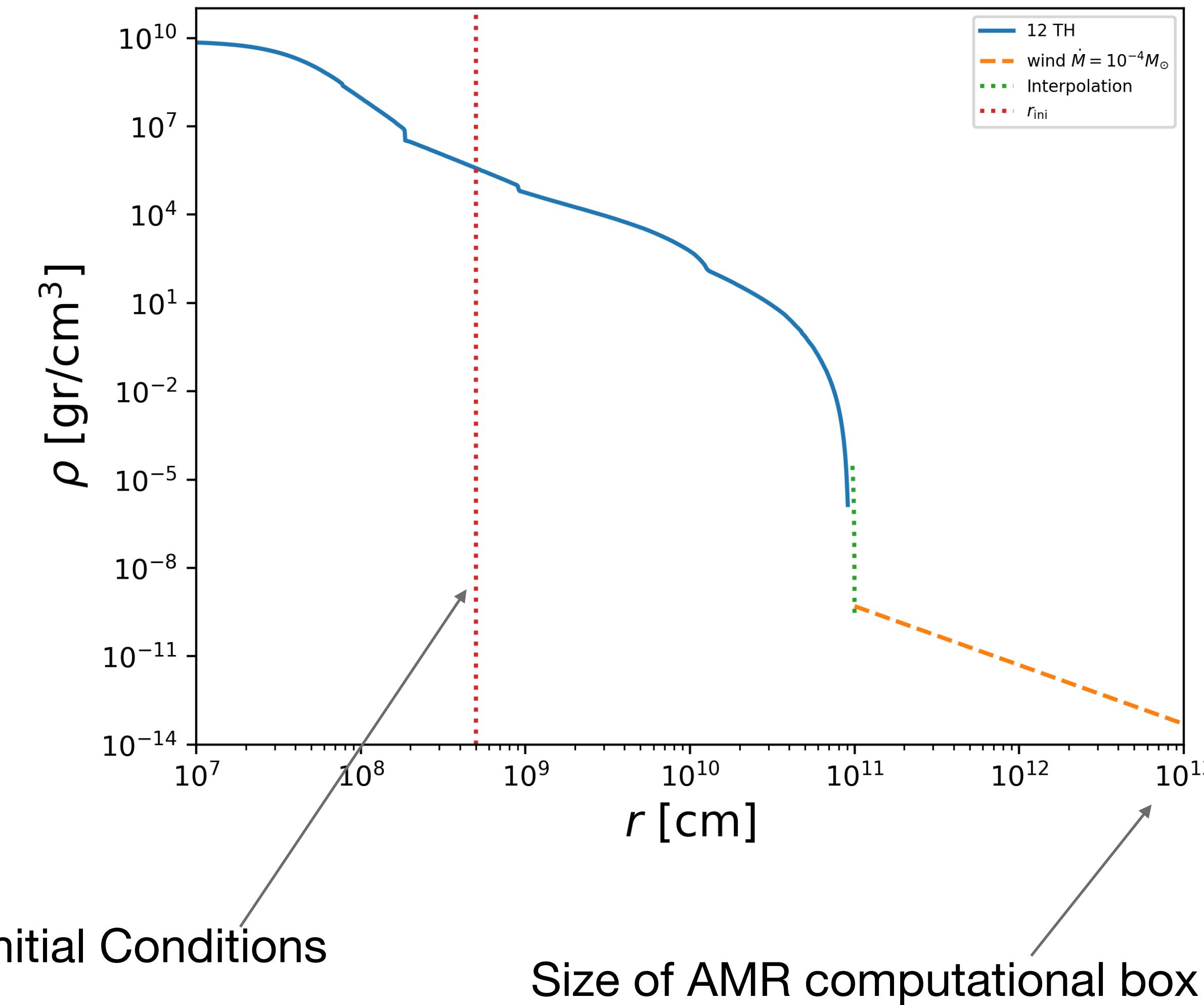
$$D = \Gamma \rho$$

$$m_j = D \hbar \Gamma v_j$$

$$\tau = D \hbar \Gamma c^2 - p - D c^2$$

# Initial conditions

(Mezcal Code: De Colle et al. 2012)



- Stellar striped envelope WR (Woosley & Heger 2006)
- AMR computational cylindrical box 2D: 40 x 40 cells
  - Minimal size: 4e-6 cm
- Jets dominated by pressure
  - Initial Lorentz factor = 10
  - Asymptotic Lorentz factor = 100

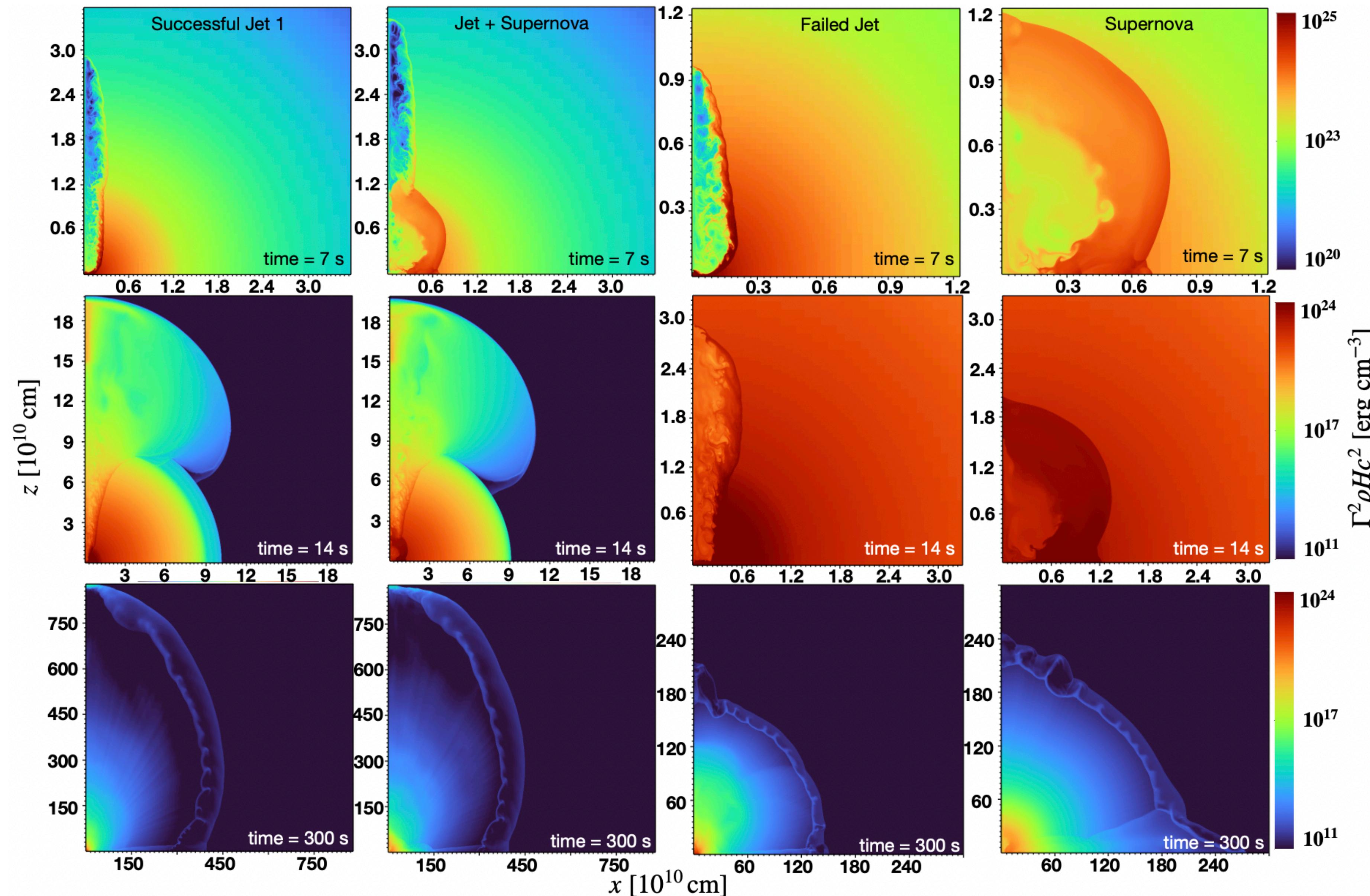
$$\rho_j = \frac{L_j}{\Gamma_\infty \Gamma_j v_j c^2 \Delta S}$$

$$P_j = \frac{\rho_j c^2}{4} \left( \frac{\Gamma_\infty}{\Gamma_j} - 1 \right)$$

(Urrutia, De Colle & López-Cámarra 2022)

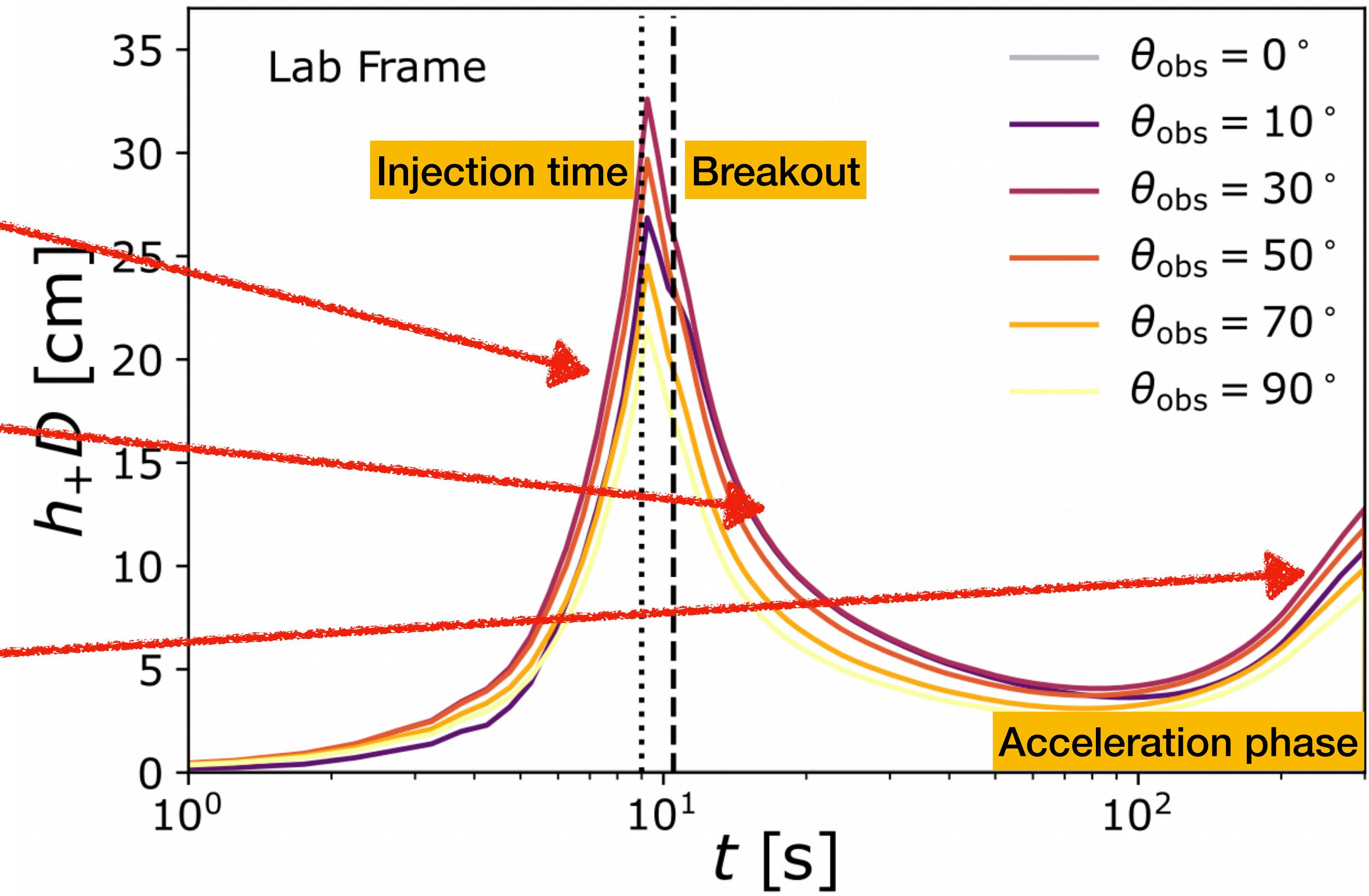
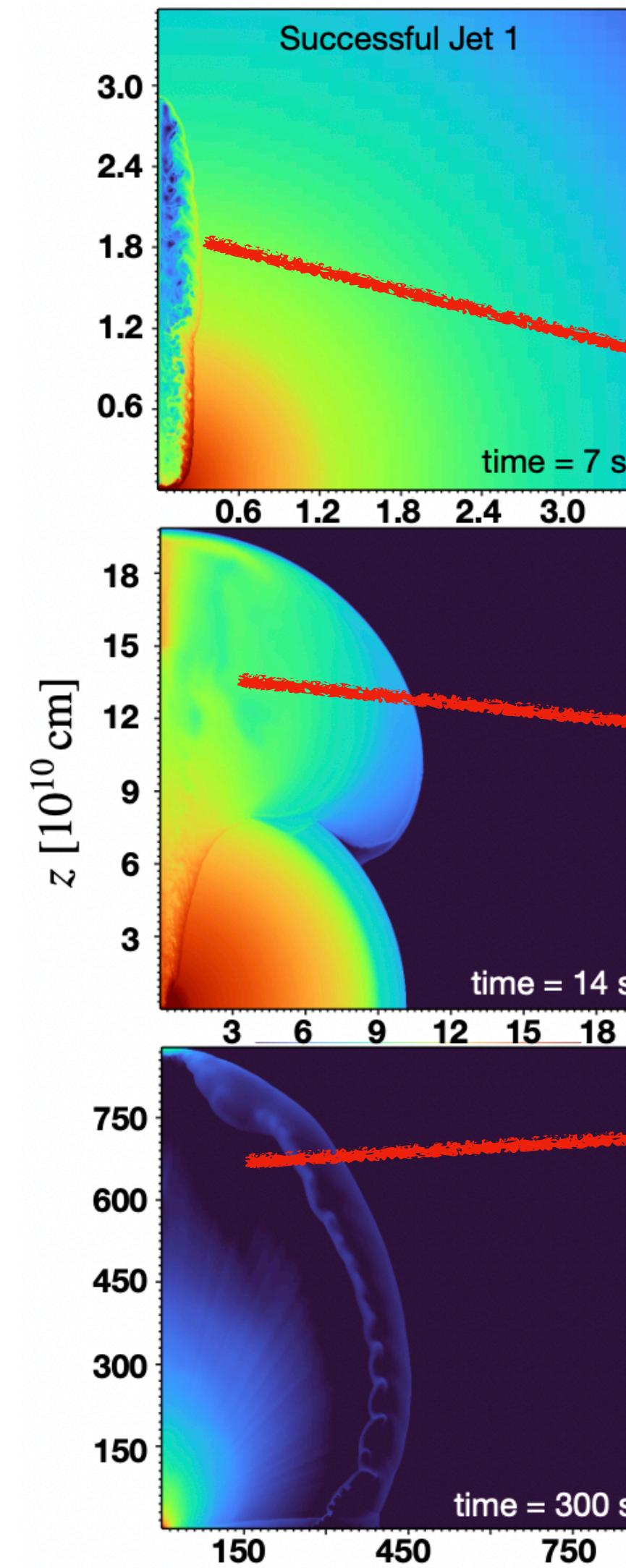
Scenario	$t_{\text{inj}}$ (s)	Energy (erg)
Successful jet	10	$10^{51}$
Successful jet	2.5	$10^{52}$
Failed jet	10	$10^{51}$
Supernova	1	$10^{52}$
Jet + Supernova	10	$10^{51}$

# Jet dynamics

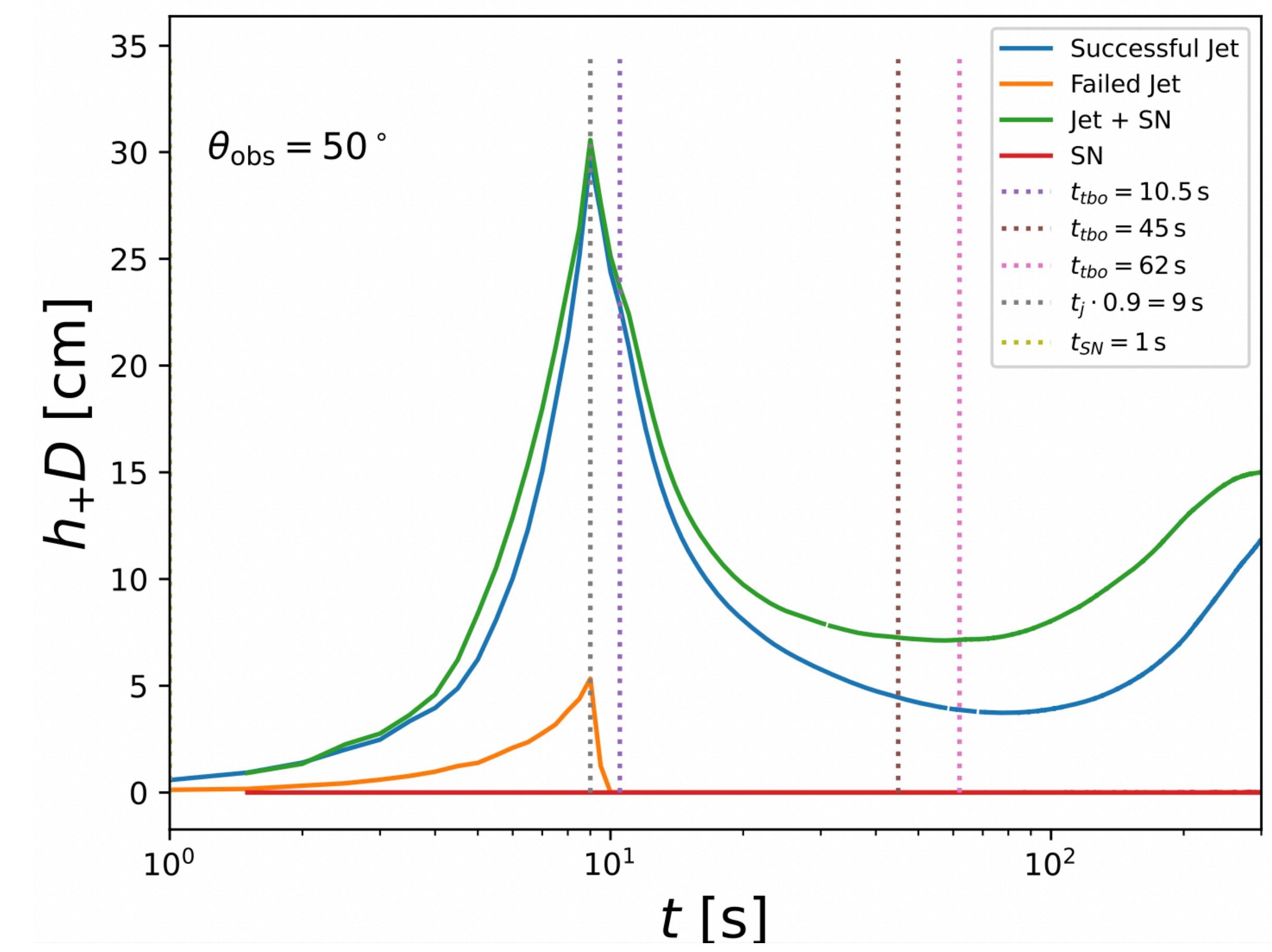
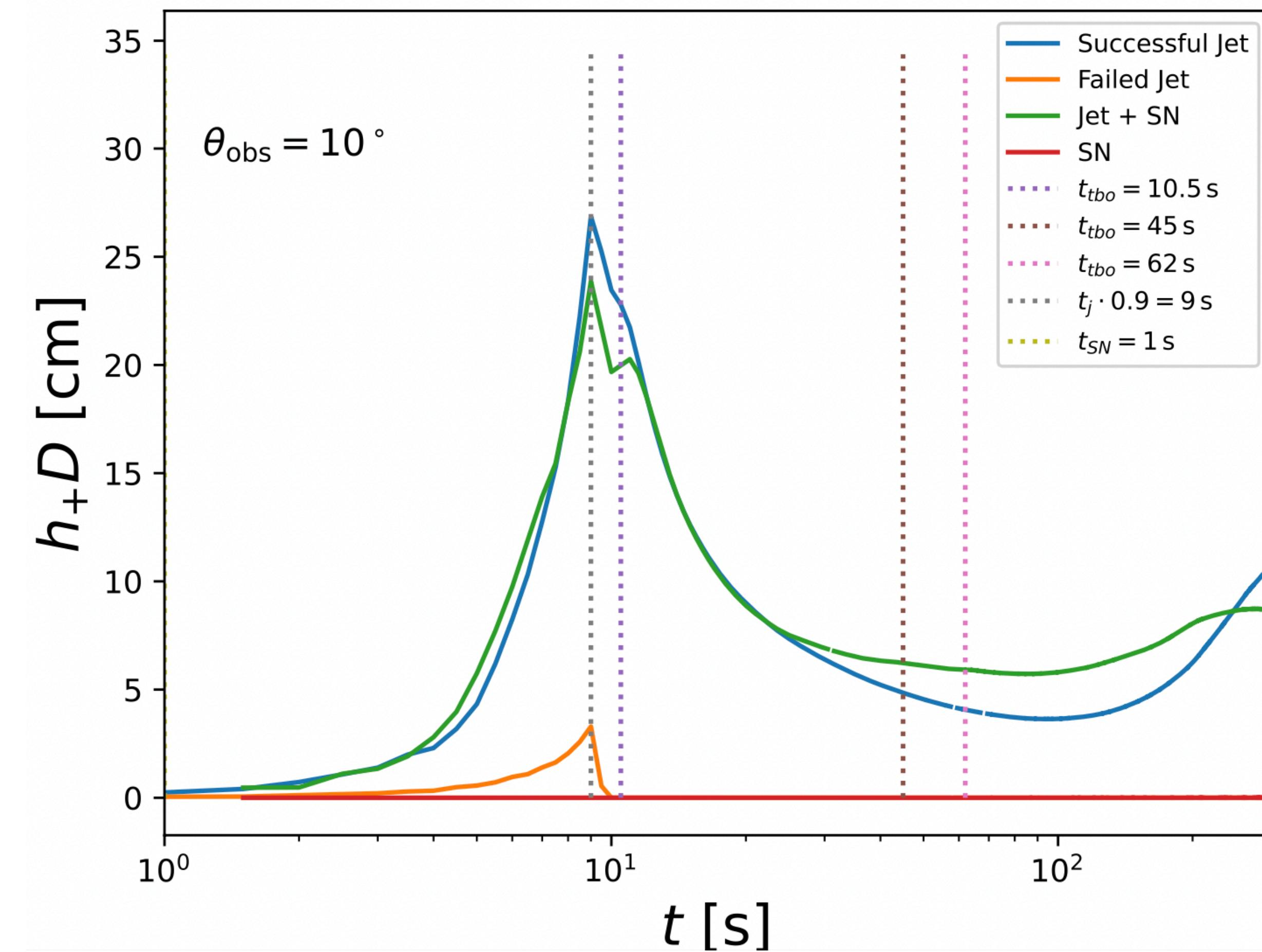


# Successful jet - GW signal

$t = t_{\text{obs}}$

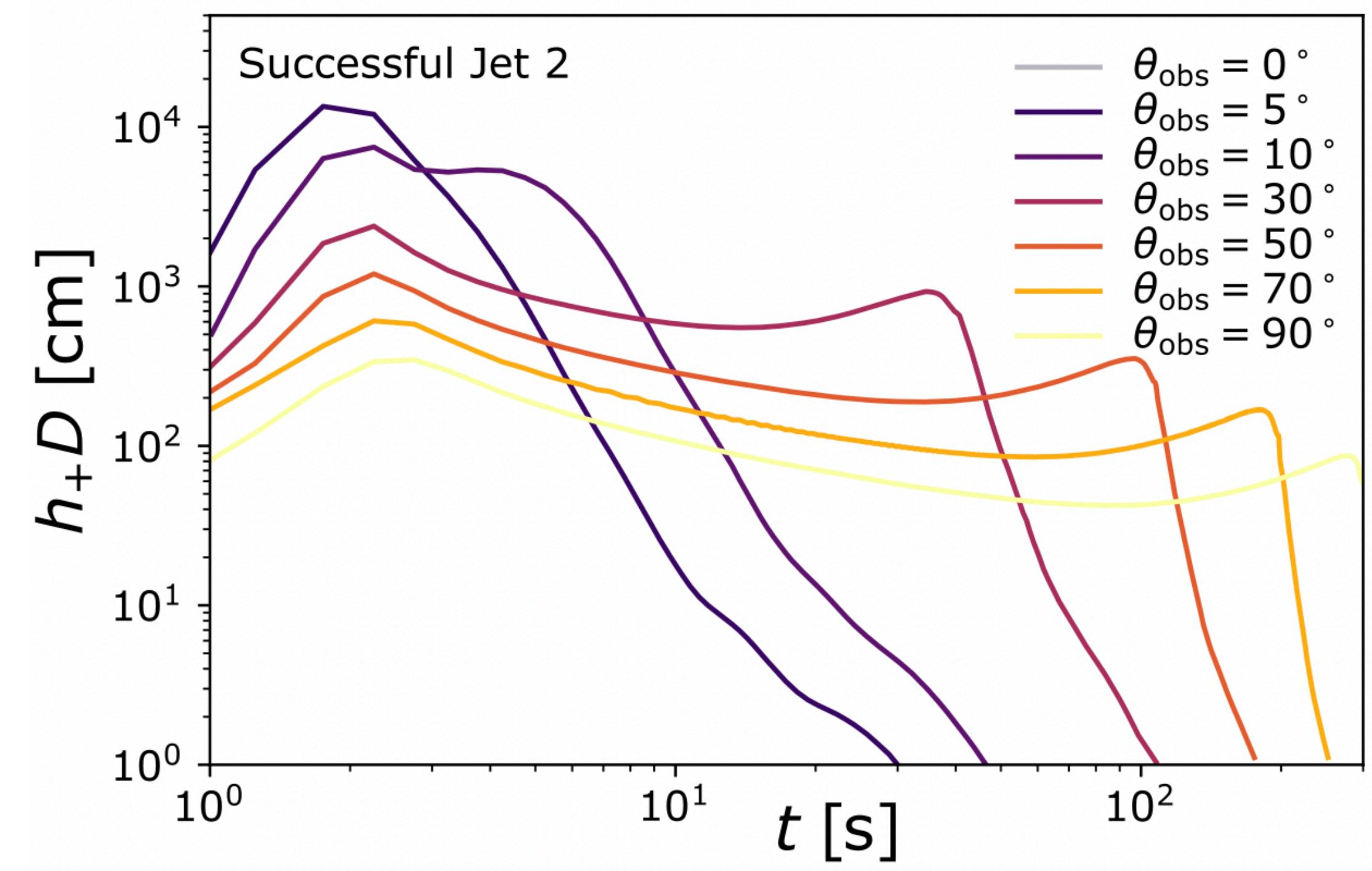
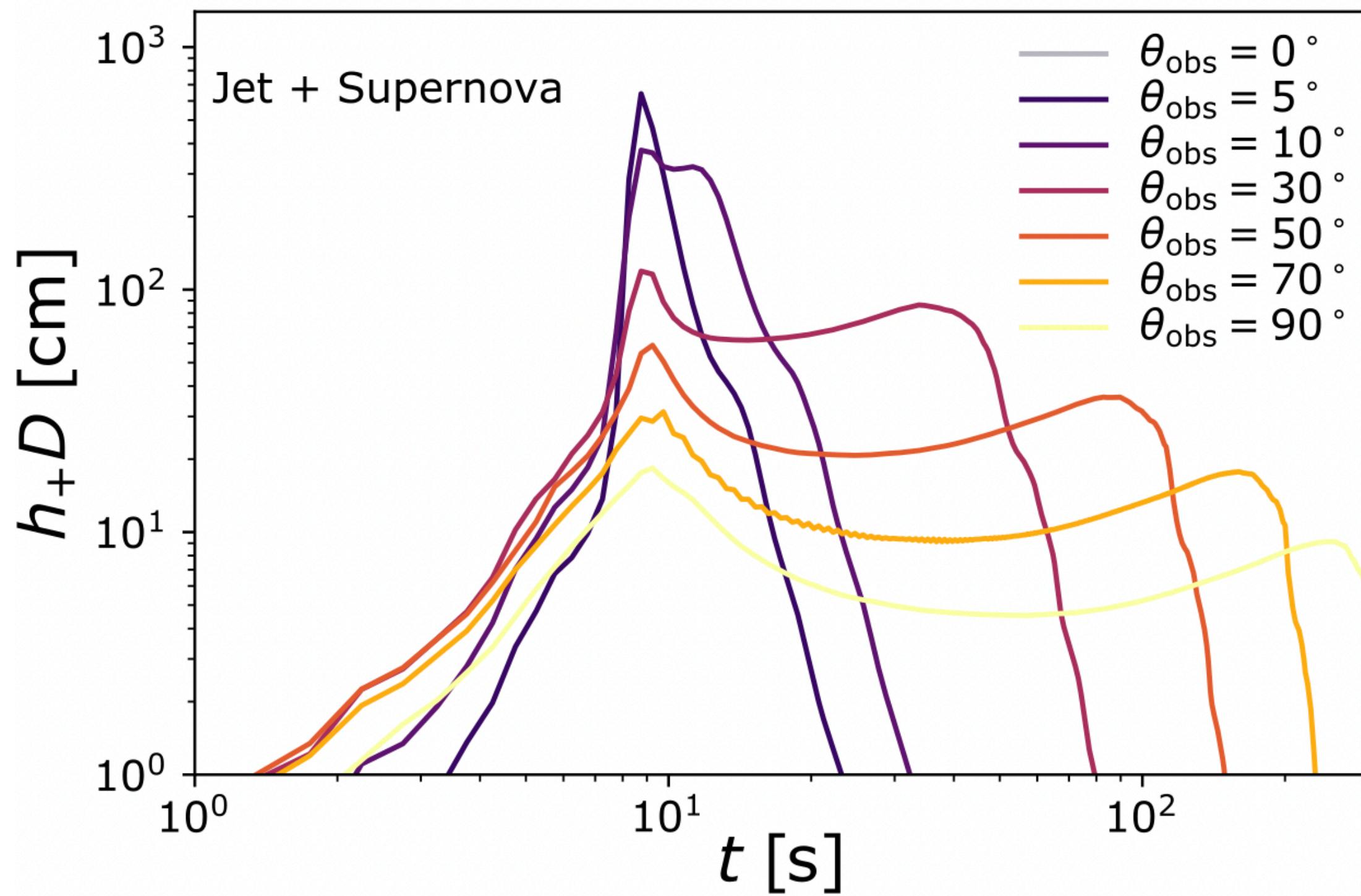


# All models $t = t_{\text{obs}}$



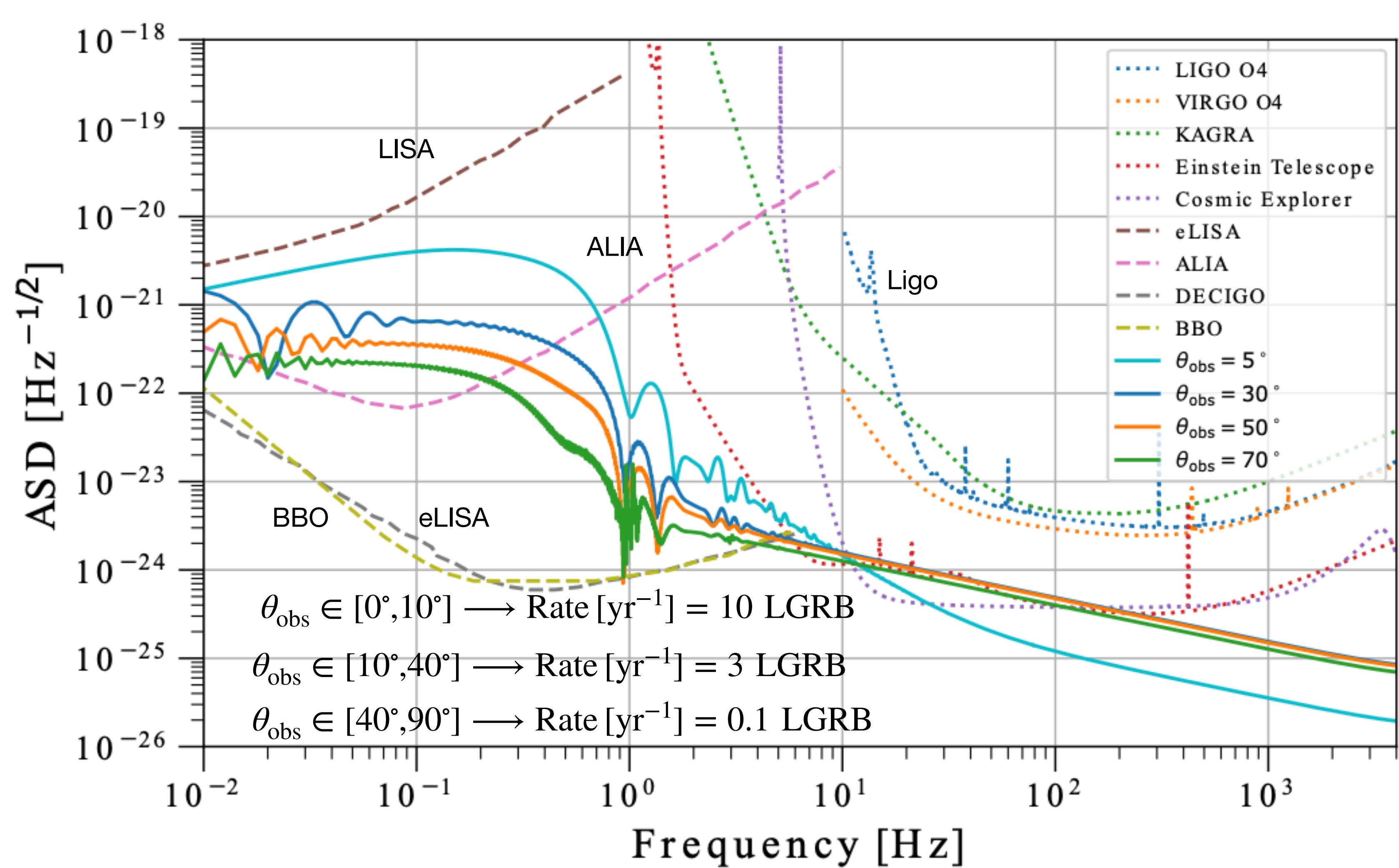
# GW signal

$$t_{\text{obs}} = t - \cos \phi \sin \theta_{\text{obs}} R/c - \cos \theta_{\text{obs}} z/c$$



$$ASD = 2f^{1/2} |\tilde{h}(f)|$$

# Detectability



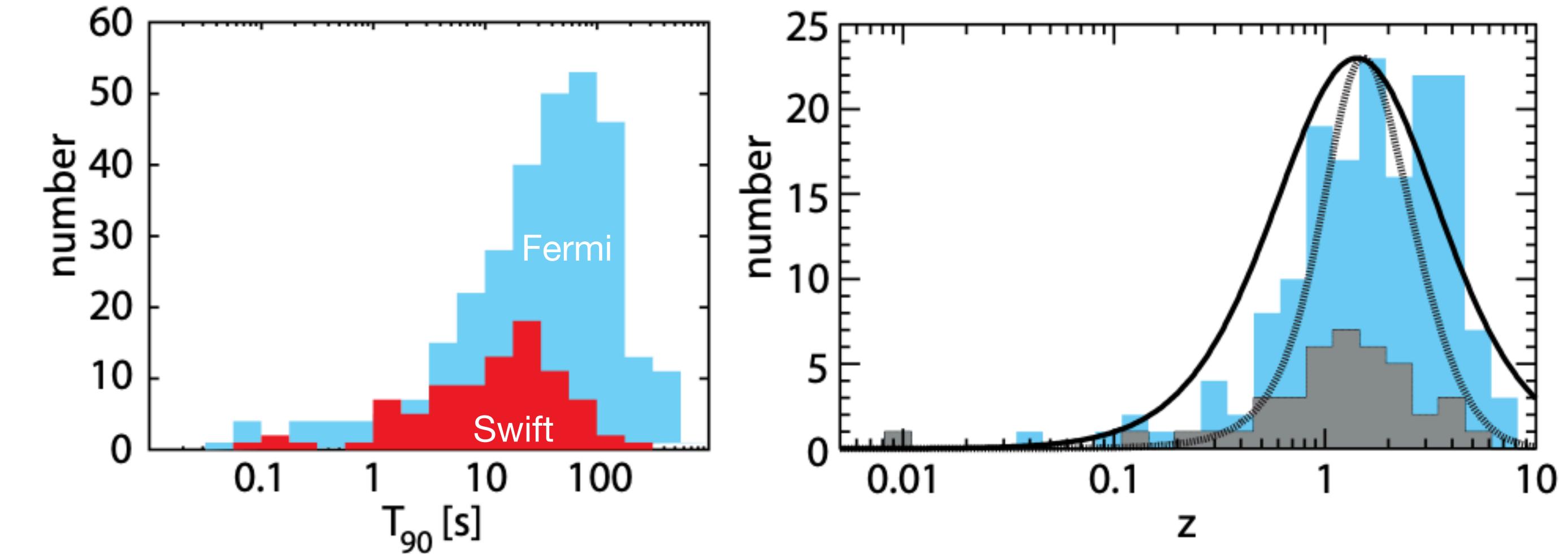
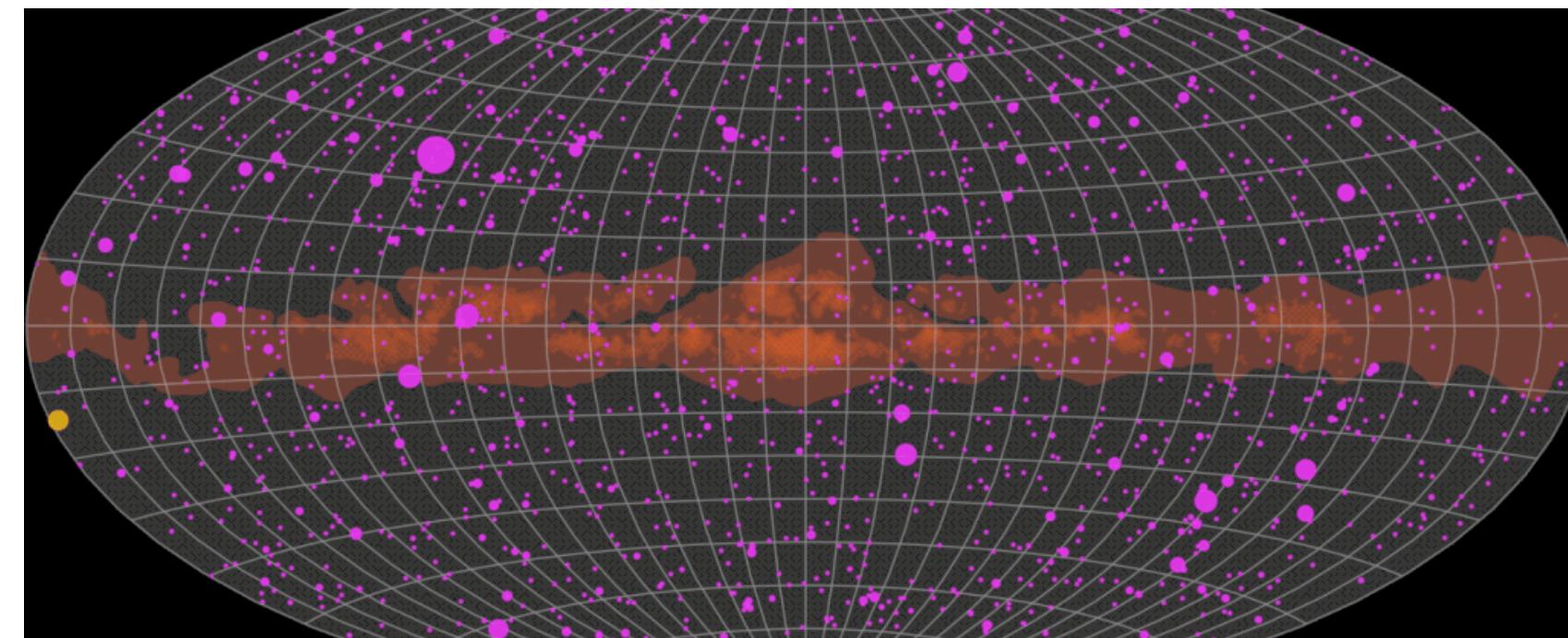
Sensitivity curves from Moore et al. 2014

$$h \propto \frac{E}{Dc^4}$$

$$E = 10^{52} \text{ erg}$$

$$D = 1 \text{ Mpc}$$

# Detectability

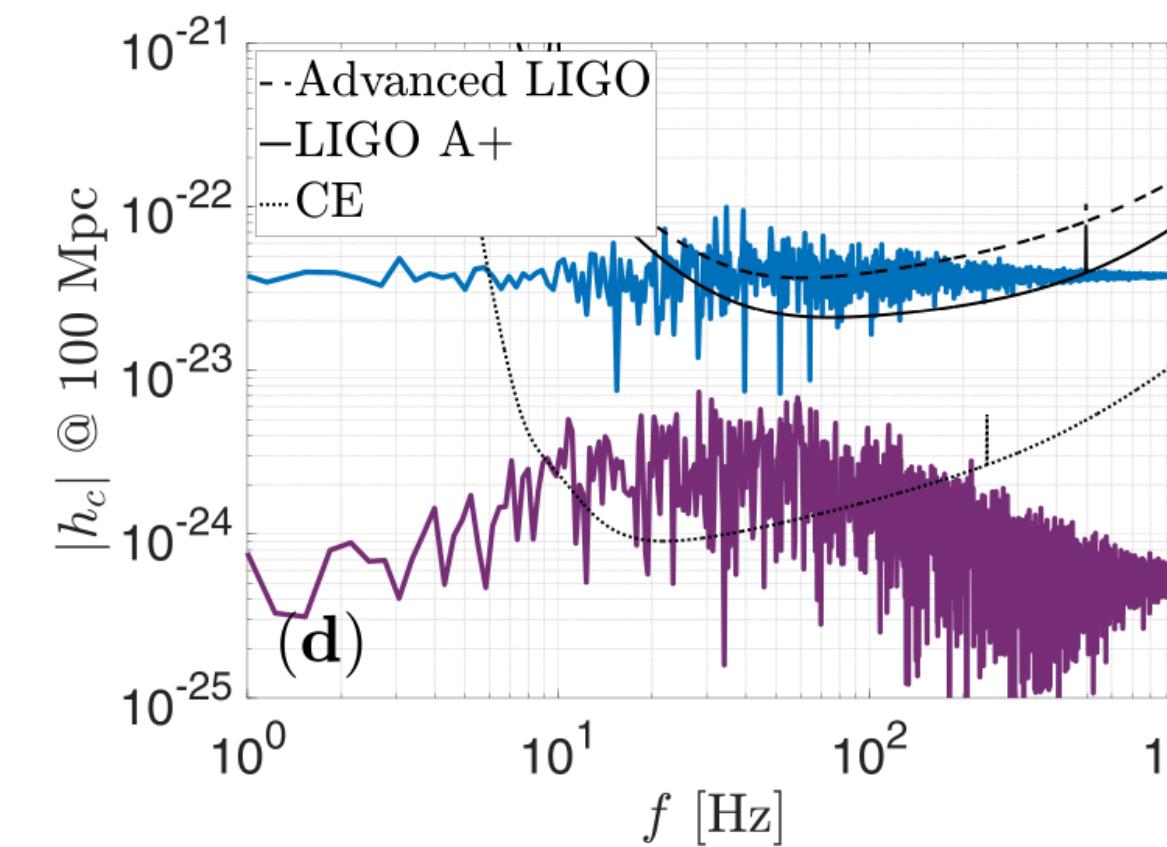
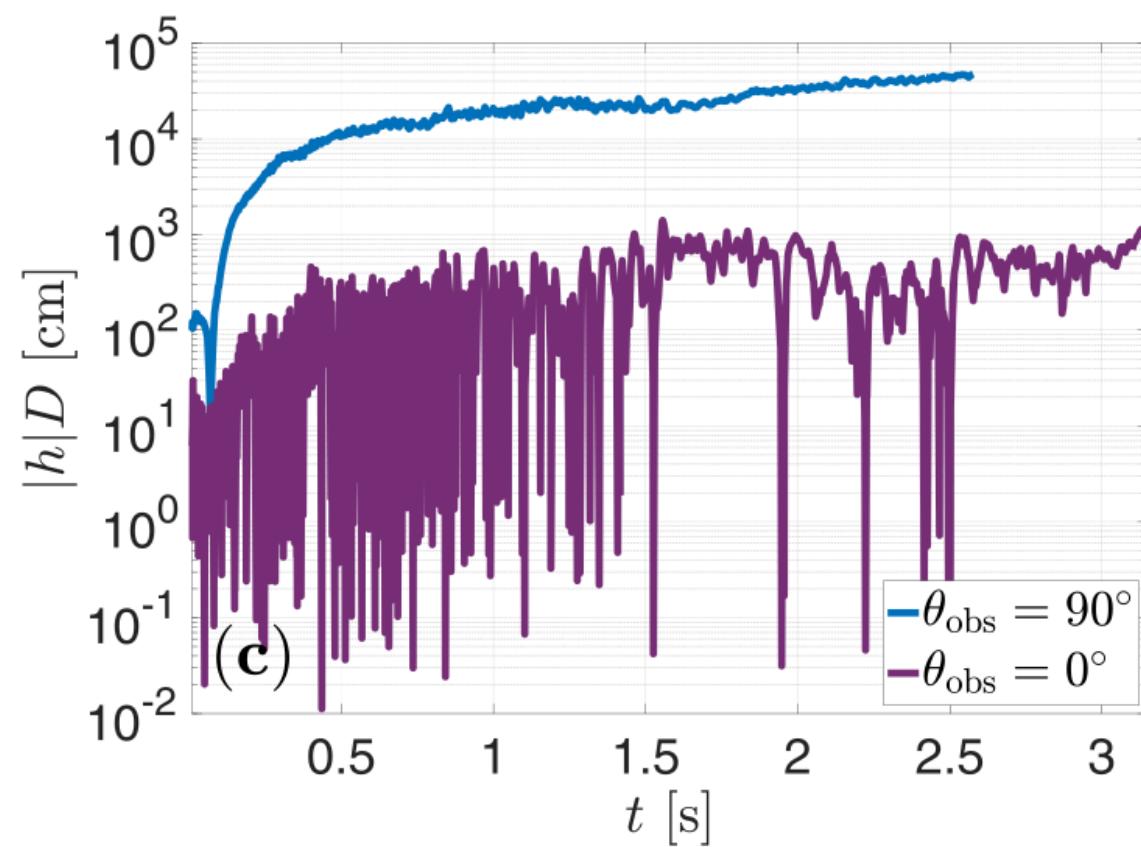
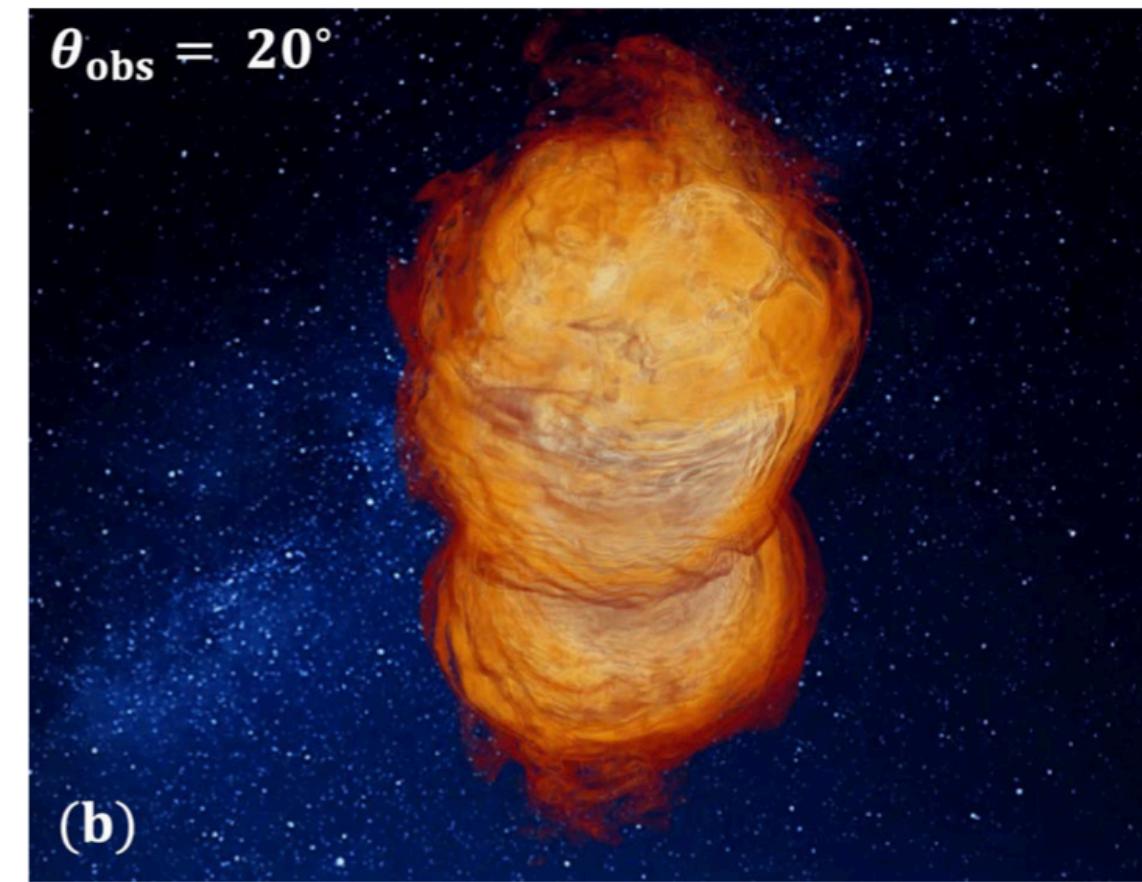
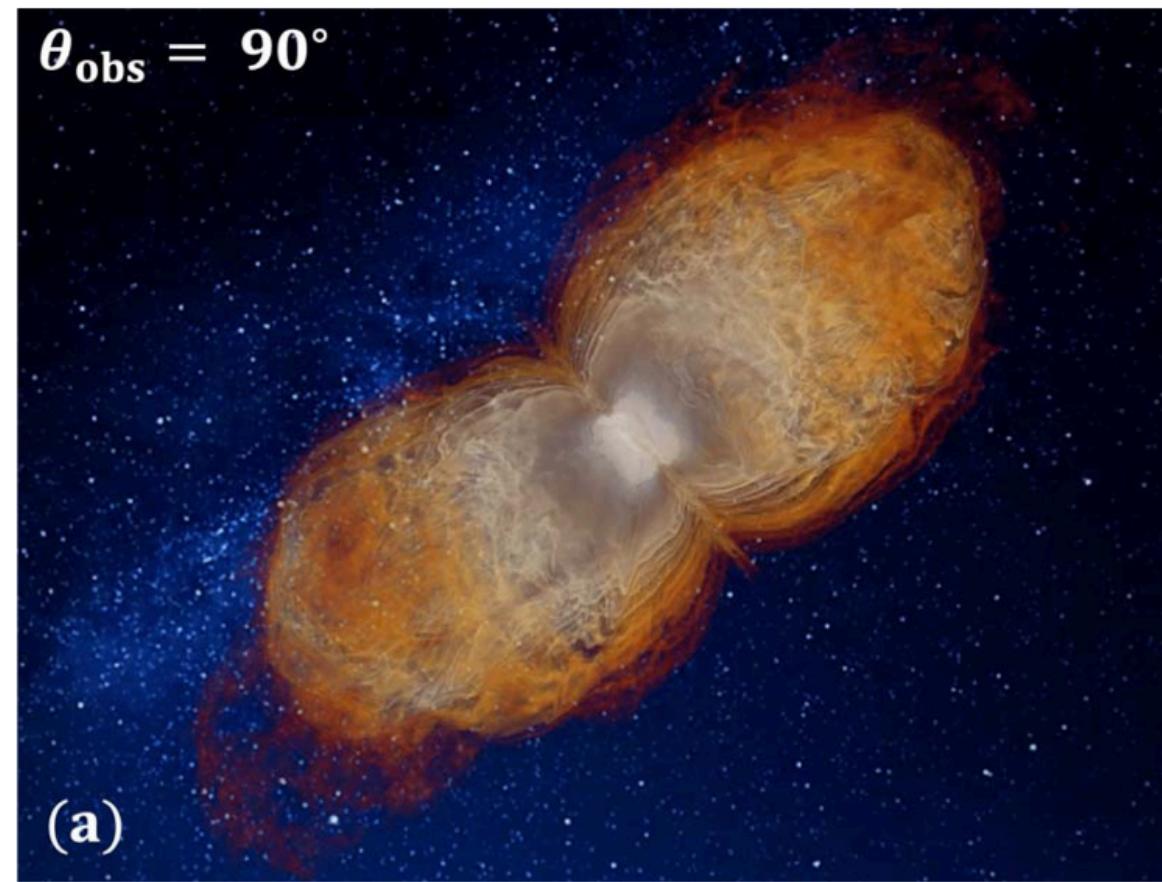


Gehrels, Ramirez-Ruiz & Fox (2009)

Detector	Distance [Mpc]			Rate [ $\text{yr}^{-1}$ ]		
	$5^\circ$	$70^\circ$	$0^\circ - 10^\circ$	$10^\circ - 40^\circ$	$40^\circ - 90^\circ$	
LIGO O4	$1.5 \times 10^{-2}$	$5.1 \times 10^{-2}$	$1.5 \times 10^{-12}$	$1.9 \times 10^{-10}$	$4.2 \times 10^{-10}$	
VIRGO O4	$2.2 \times 10^{-2}$	$2.2 \times 10^{-2}$	$7.3 \times 10^{-13}$	$1.8 \times 10^{-11}$	$3.6 \times 10^{-11}$	
KAGRA	$7.3 \times 10^{-3}$	$2.3 \times 10^{-2}$	$1.6 \times 10^{-14}$	$2.1 \times 10^{-12}$	$5.0 \times 10^{-12}$	
Einstein Telescope	$3.5 \times 10^{-1}$	$5.0 \times 10^{-1}$	$3.9 \times 10^{-10}$	$2.3 \times 10^{-8}$	$5.3 \times 10^{-8}$	
Cosmic Explorer	$3.0 \times 10^{-1}$	$5.3 \times 10^{-1}$	$3.4 \times 10^{-10}$	$2.8 \times 10^{-8}$	$6.4 \times 10^{-8}$	
eLISA	$8.5 \times 10^{-2}$	$1.5 \times 10^{-2}$	$5.5 \times 10^{-11}$	$3.7 \times 10^{-10}$	$4.0 \times 10^{-11}$	
ALIA	6.4	$3.7 \times 10^{-1}$	$1.3 \times 10^{-5}$	$1.2 \times 10^{-5}$	$4.5 \times 10^{-7}$	
DECIGO	$6.0 \times 10^2$	$1.8 \times 10^1$	7.5	2.2	$1.0 \times 10^{-1}$	
BBO	$6.0 \times 10^2$	$2.1 \times 10^1$	7.9	2.5	$1.2 \times 10^{-1}$	

Urrutia, De Colle, Moreno & Zanolin (2022)

# High resolution 3D simulation



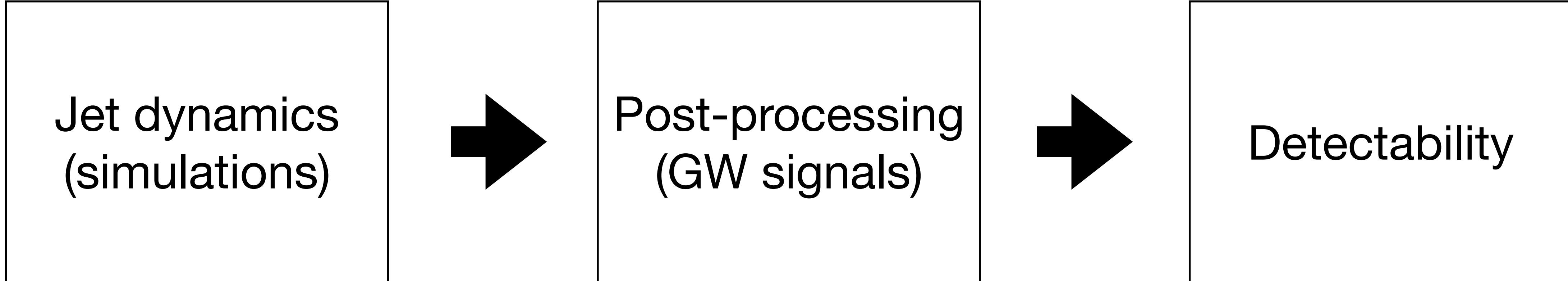
$$h \approx 10^{-22} \frac{40 \text{ Mpc}}{D} \frac{E}{10^{53} \text{ erg}}$$

$$E_{\text{cocoon}} = 10^{52} - 10^{53} \text{ erg}$$

$\Delta t \propto 10^{-4} \text{ s}$  (Temporal resolution)

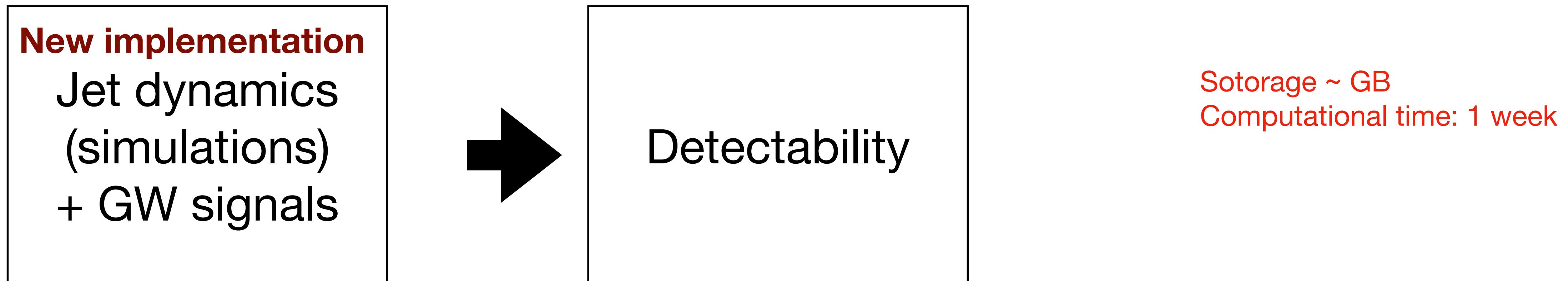
Storage  $\sim$  Petabytes

# Currently methodology



Sotorage ~ TB  
Computational time: 3 days

# New methodology



Sotorage ~ GB  
Computational time: 1 week

# Estimation of GW signals during the jet propagation (not post-processing)

$\Delta t \propto 10^{-4}$  s (Temporal resolution)

Ram memory ~ GB

Storage ~ GB

$$ASD = 2f^{1/2} |\tilde{h}(f)|$$

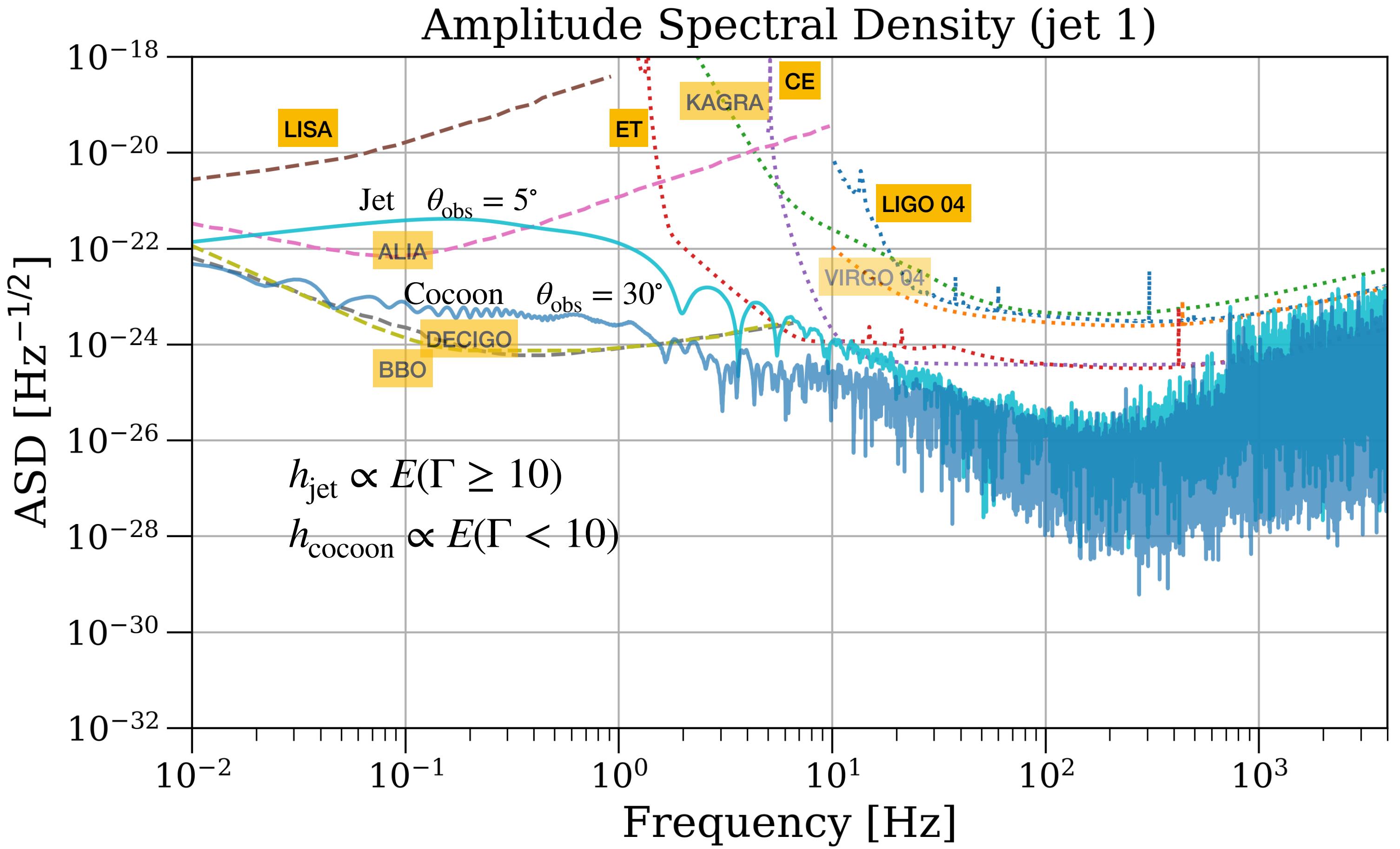
$$E_j = 10^{51} \text{ erg}$$

$$t_j = 10 \text{ s}$$

$$R_\star = 10^{11} \text{ cm}$$

$$D_{\text{obs}} = 1 \text{ Mpc}$$

Urrutia (in Prep)



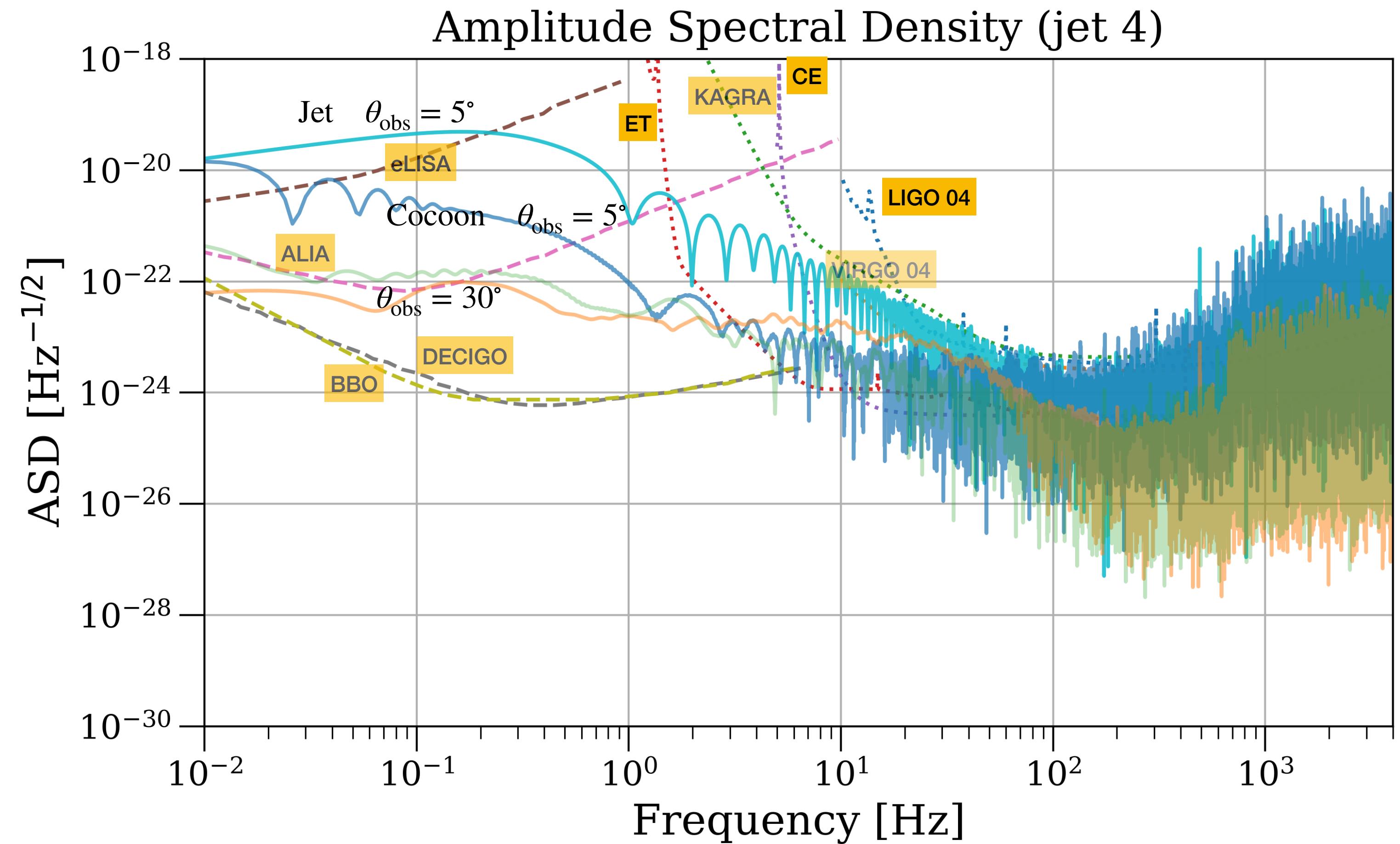
# Estimation of GW signals during the jet propagation (not post-processing)

$$E_j = 10^{52} \text{ erg}$$

$$t_j = 2.5 \text{ s}$$

$$R_\star = 10^{11} \text{ cm}$$

$$D_{\text{obs}} = 1 \text{ Mpc}$$



# Conclusions

- A new generation of observatories will observe GW signals from GRB jets.
- The rate of detection by DECIGO and BBO may be  $10 \text{ GRBs yr}^{-1} \text{ Gpc}^{-3}$
- Jet parameters: injection time,  $L(t)$ , velocity, size of GRB progenitor, acceleration region, jet observing angle are strongly connected to the shape of the GW signal.
- GW signal will provide unique information about the early jet dynamics, the progenitor and the physics of central engine.